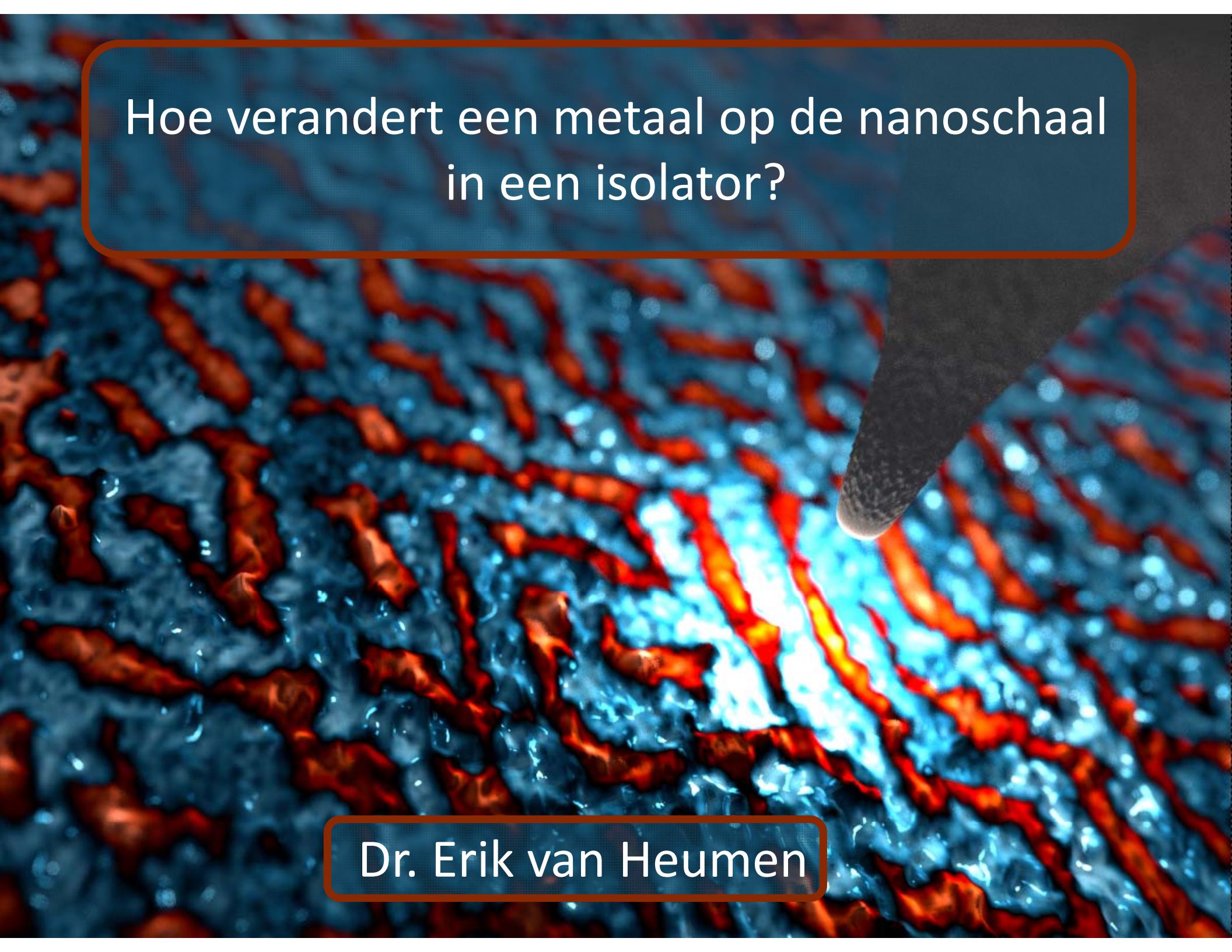


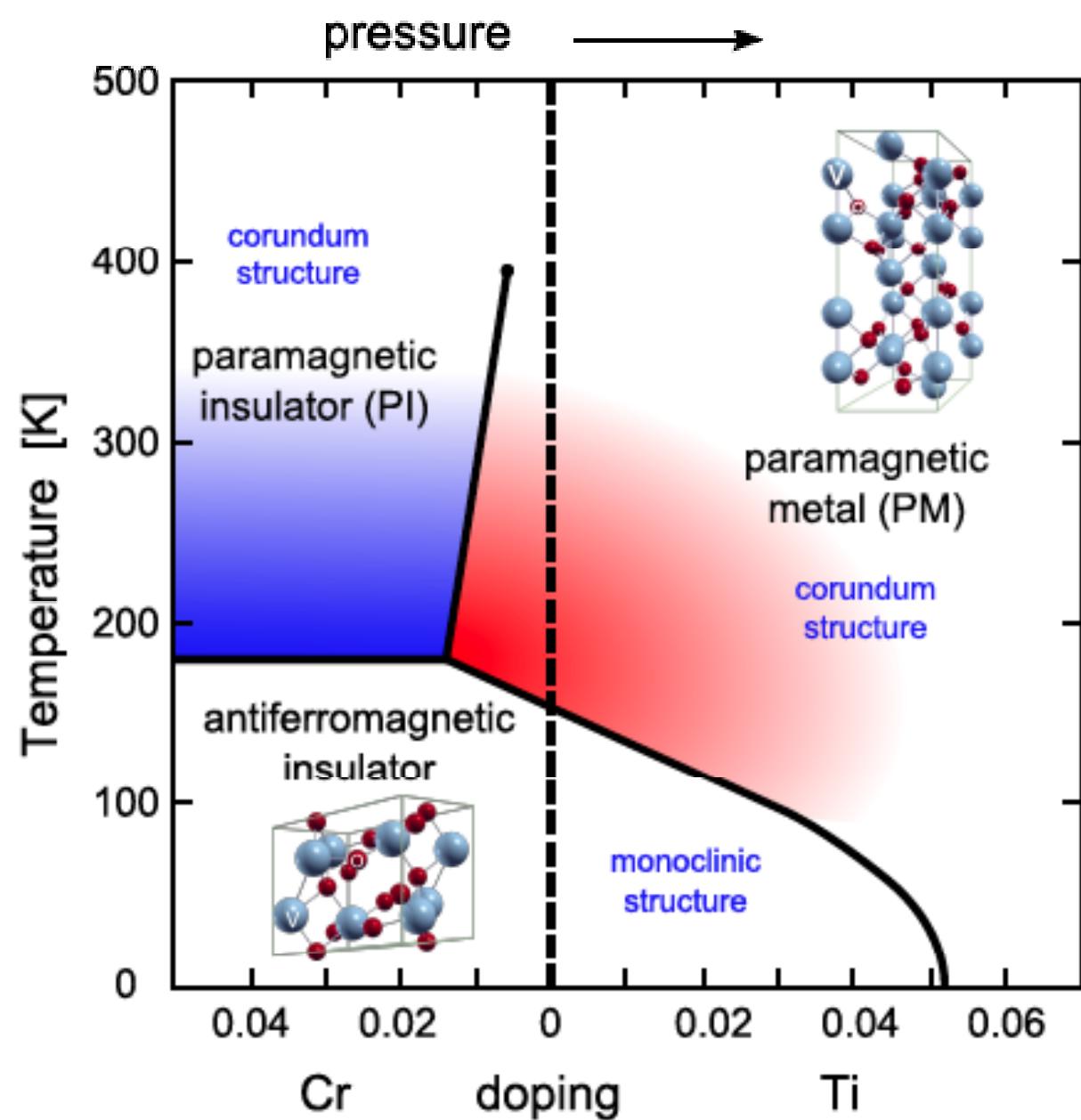
Hoe verandert een metaal op de nanoschaal  
in een isolator?



Dr. Erik van Heumen

- Hoe/waarom verandert een metaal in een isolator?
- Hoe maak je dit zichtbaar op de nanoschaal?

# Metaal-Isolator overgang in $V_2O_3$



Sterk wisselwerkend metaal  
Structurele en magnetische overgangen

Wat drijft de overgang van metaal naar isolator?

McWhan et al., PRL 23, 1384 (1969)

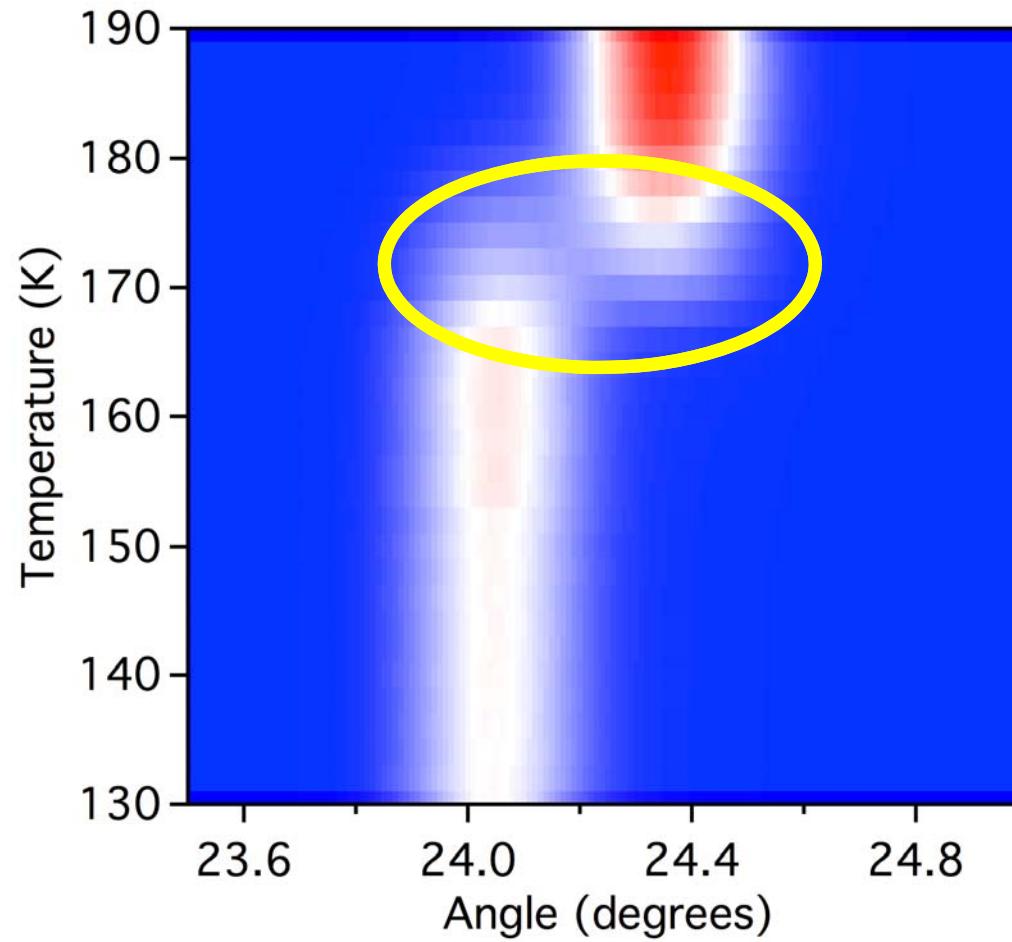
Hansmann et al. Phys. Status Solidi B 250, 1251 (2013)



# V<sub>2</sub>O<sub>3</sub> kristal structuur -

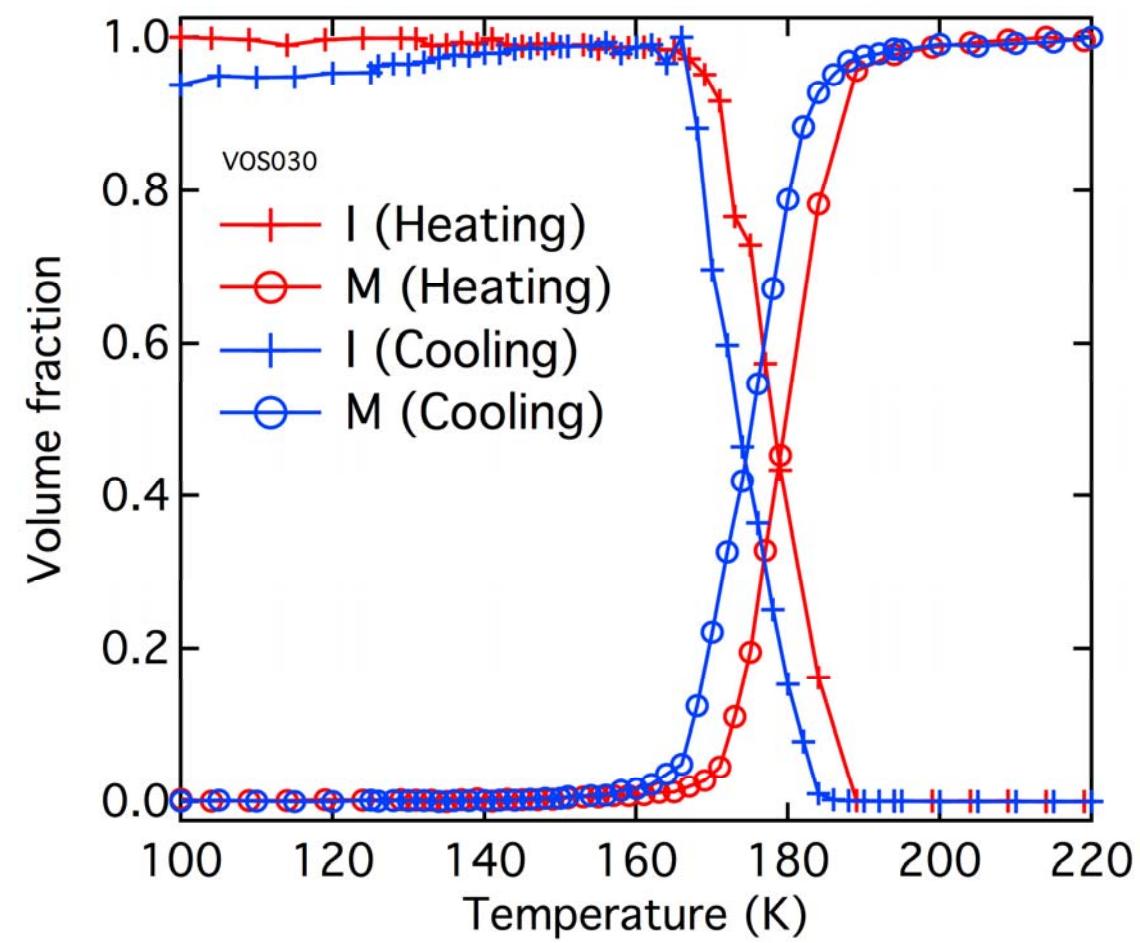
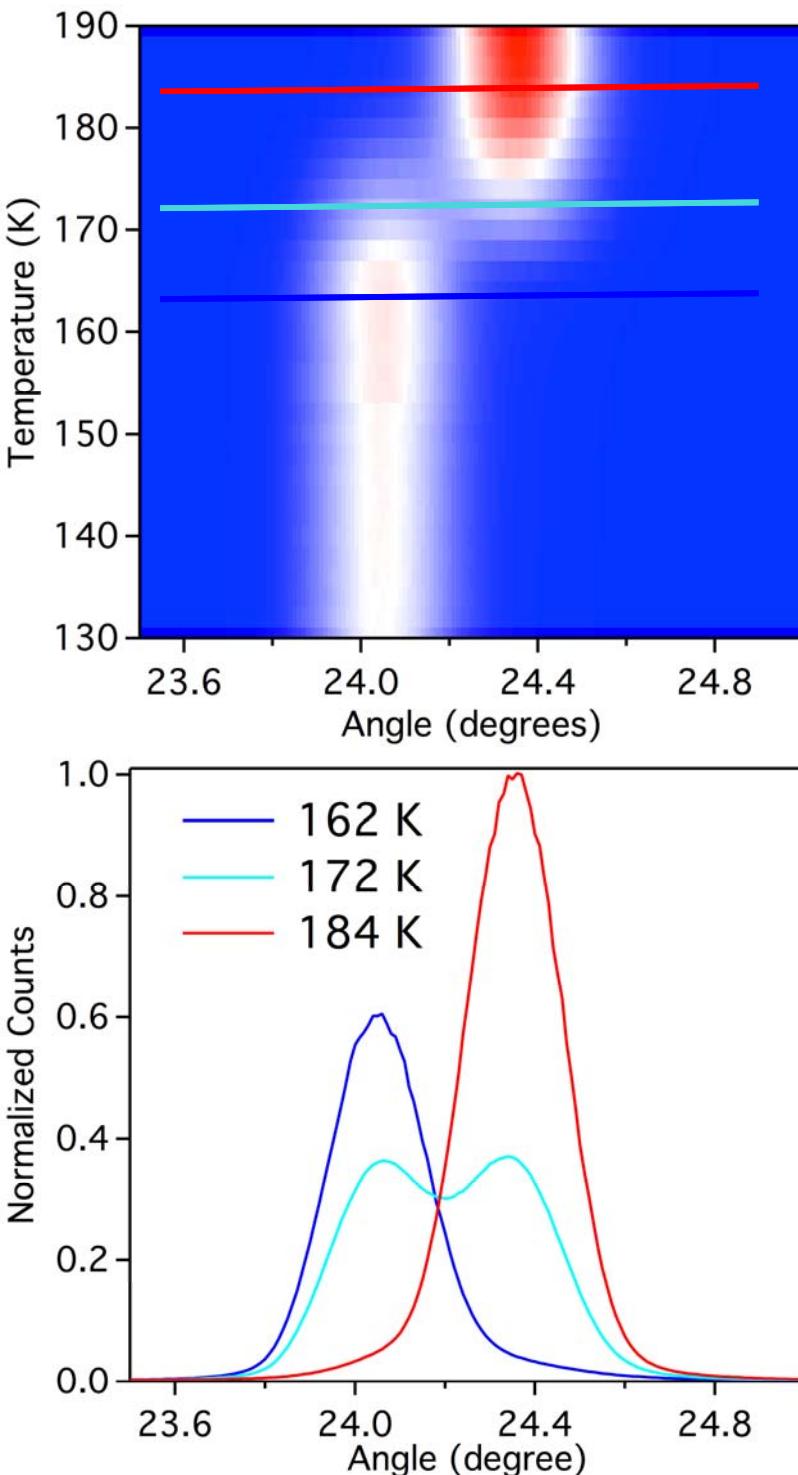
300 nm film V<sub>2</sub>O<sub>3</sub> op saffier

rontgen diffractie: ([110] and [012] peaks)



2 structuren bij dezelfde T

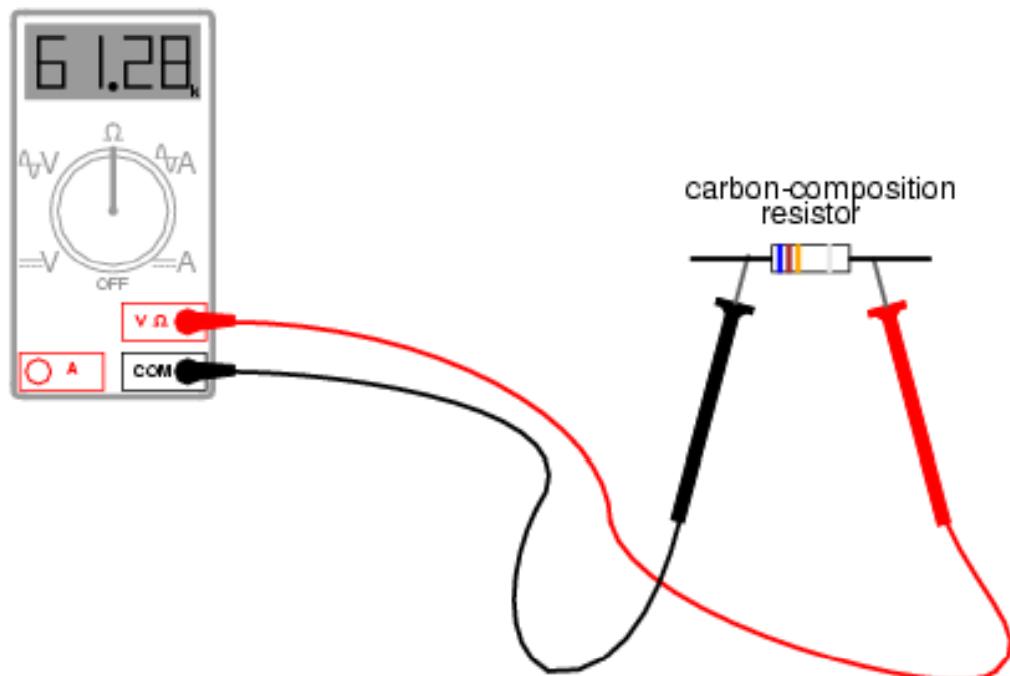
# $V_2O_3$ kristal structuur



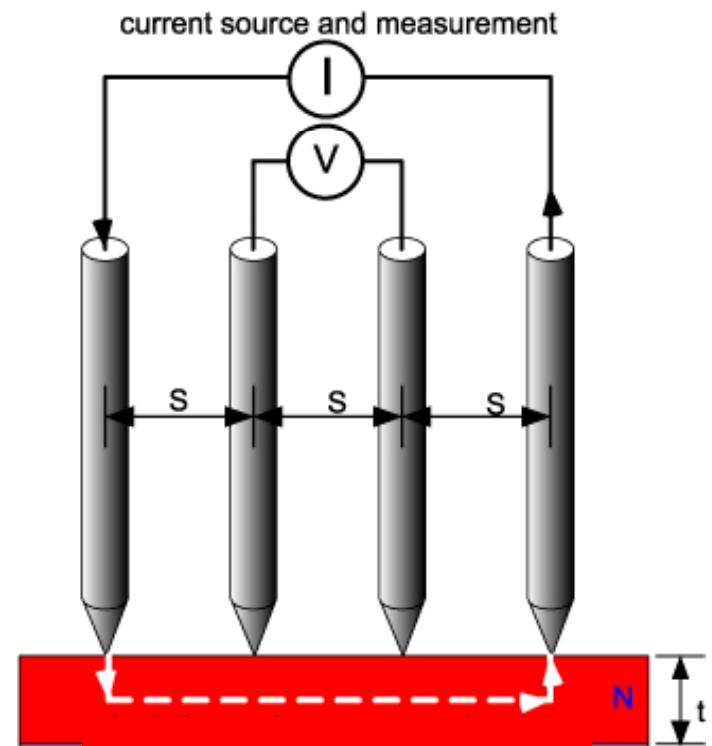
Volgen de elektronen de  
kristal structuur?

- Hoe/waarom verandert een metaal in een isolator?
- Hoe maak je dit zichtbaar op de nanoschaal?

## Methode nr. 1

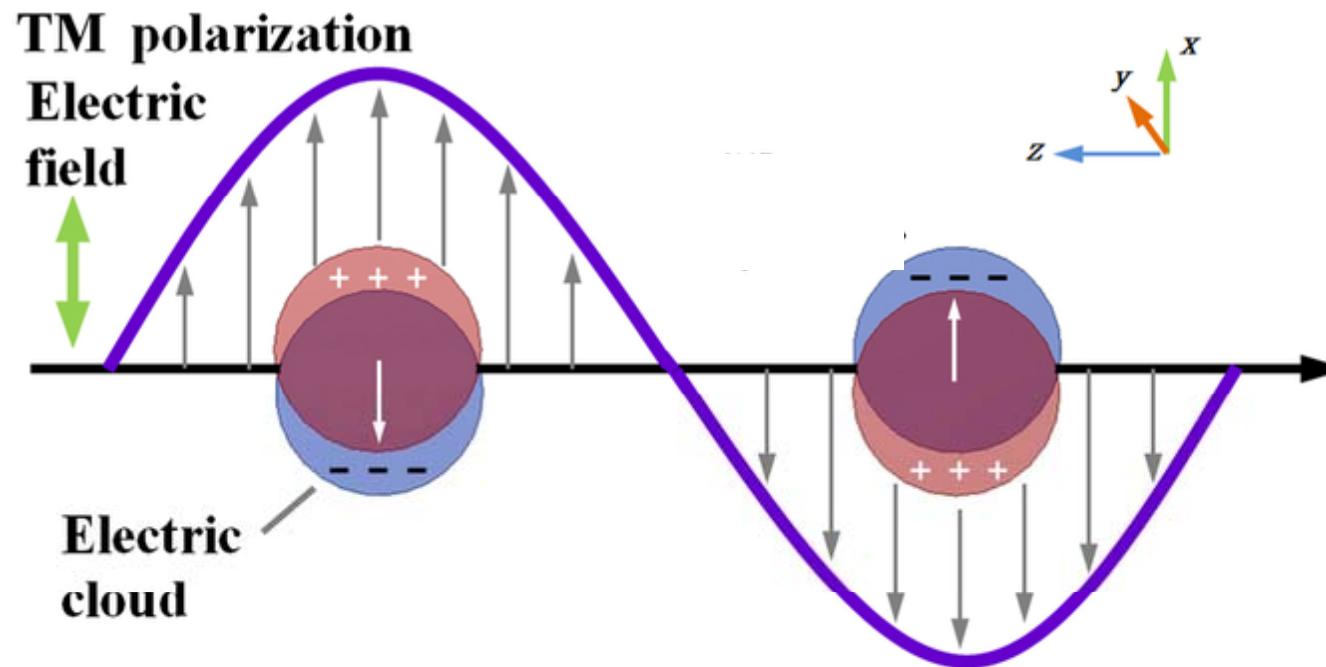


## Methode nr. 2



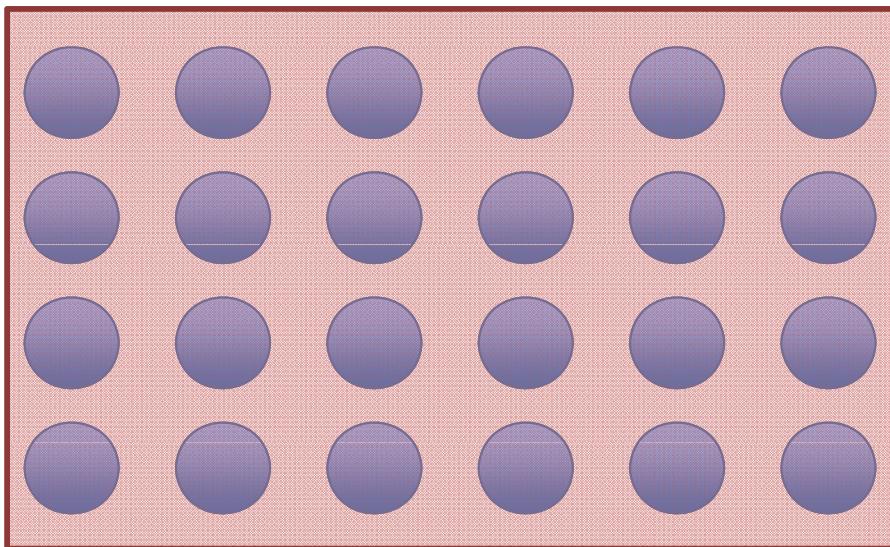
50 nm contact afstand !

- Licht (foton) is een wisselend elektromagnetisch veld!



# Het Drude model

Vrije lading



ionen



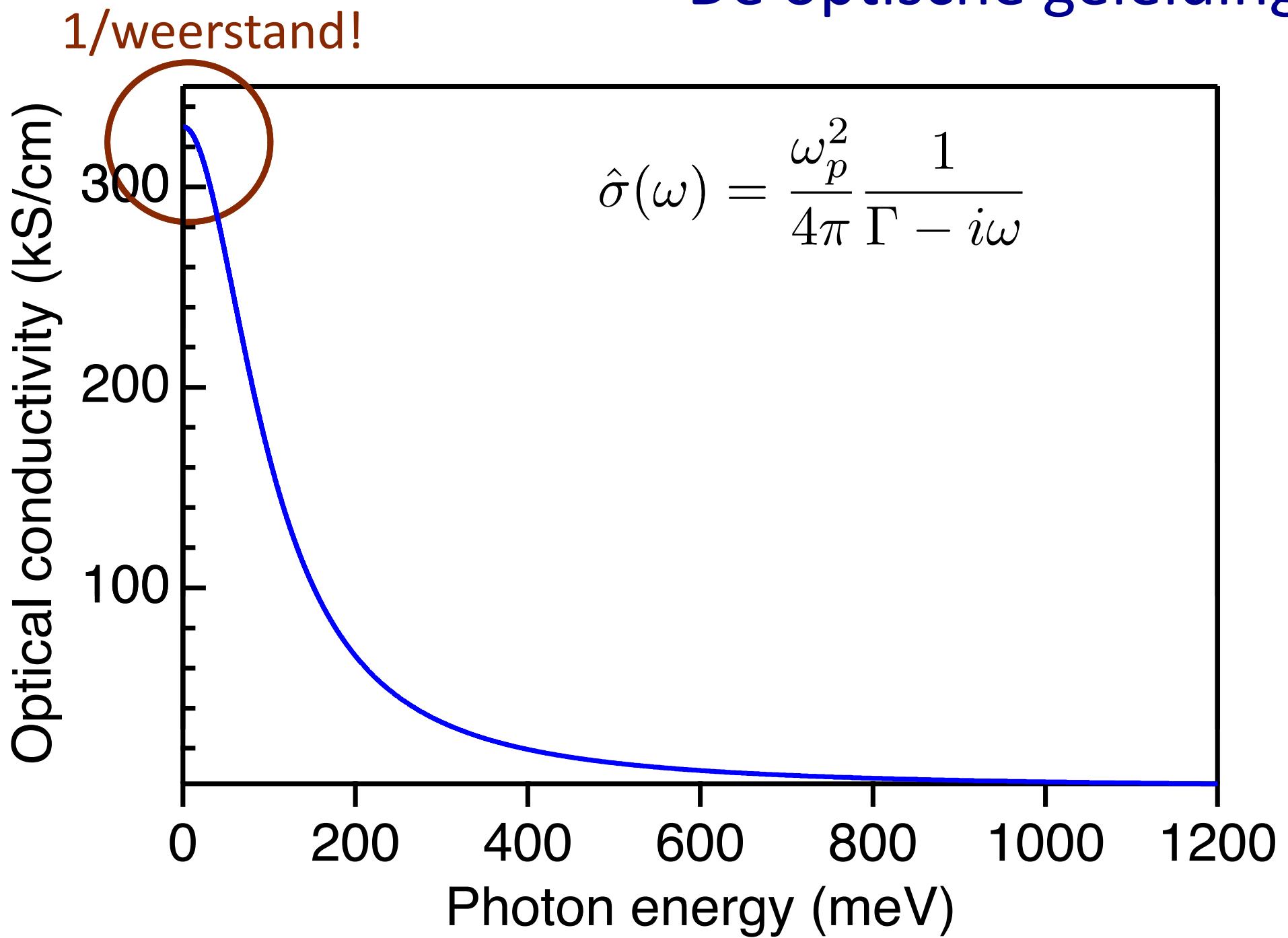
Het Drude model beschrijft metalen.



Elektronen botsen met ionen.



Paul Drude

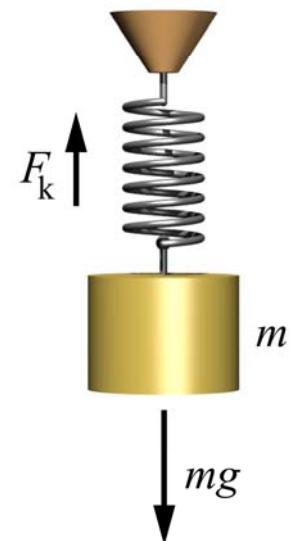


# De optische geleiding –

● Lorentz bedacht wat er gebeurde als de elektronen 'vast' zaten.

● Hij nam aan dat er een 'nieuwe' kracht was die de elektronen aan de kernen gebonden hield (wet van Hooke).

● Dit is een model voor een isolator!



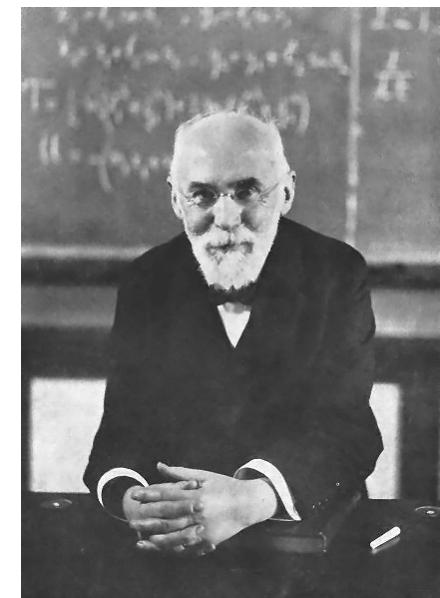
Drude

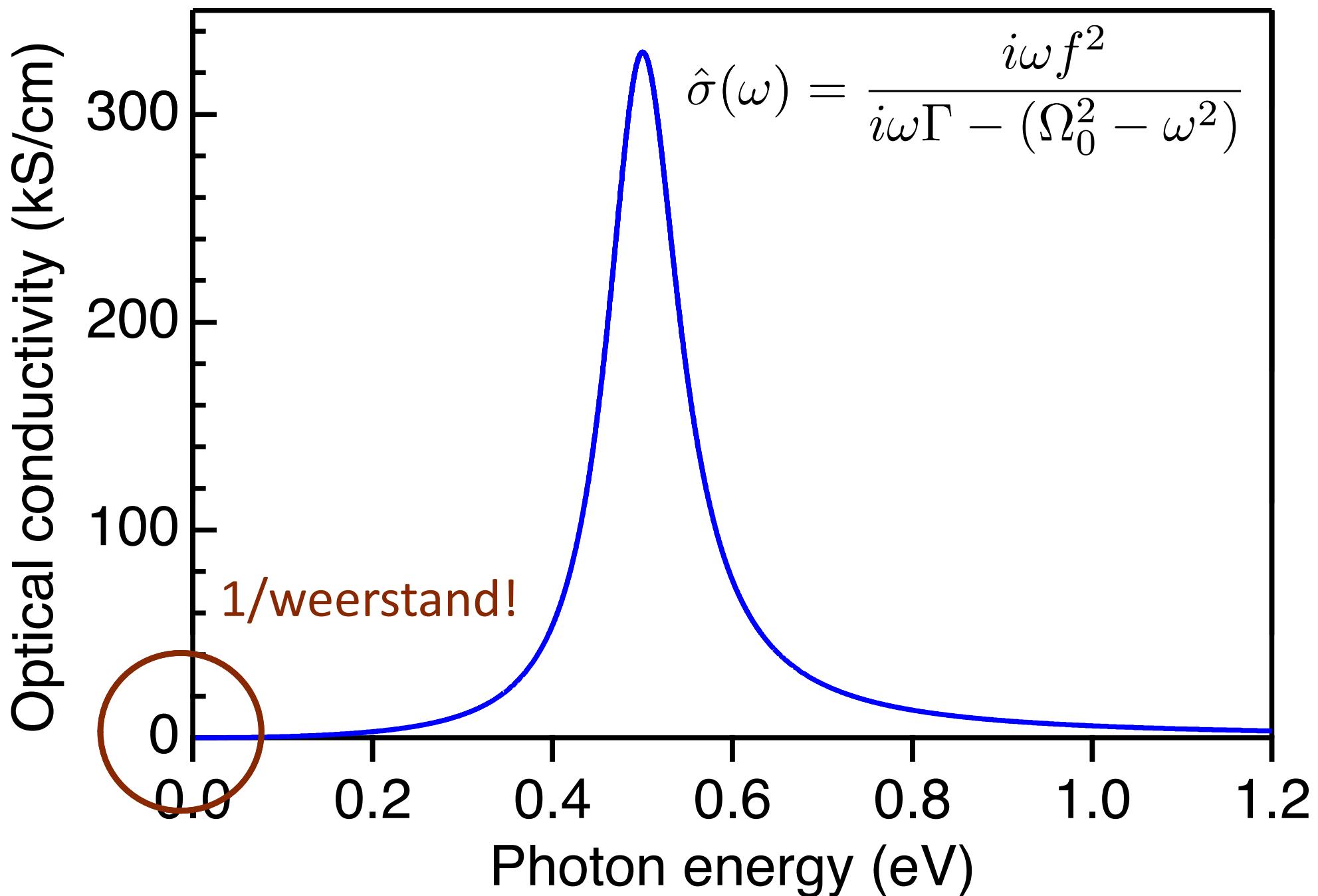
$$\hat{\sigma}(\omega) = \frac{\omega_p^2}{4\pi} \frac{1}{\Gamma - i\omega}$$

Lorentz

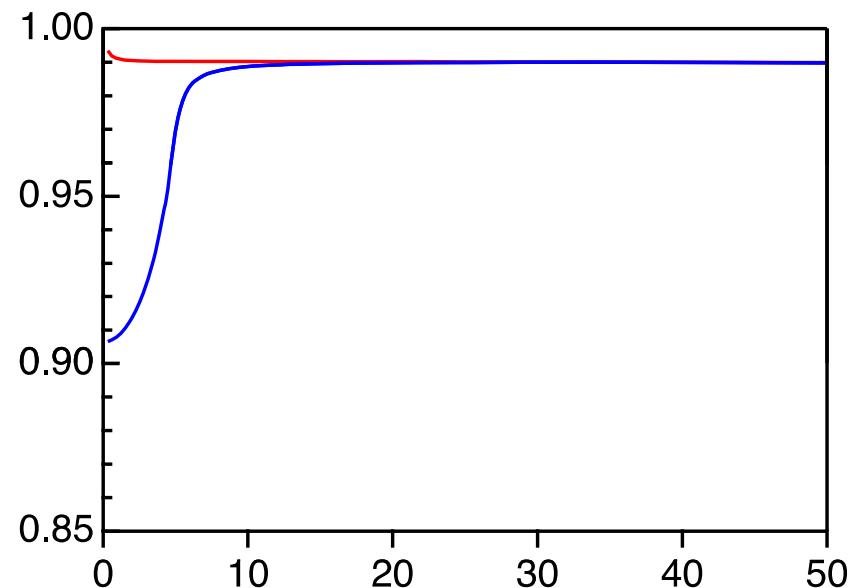
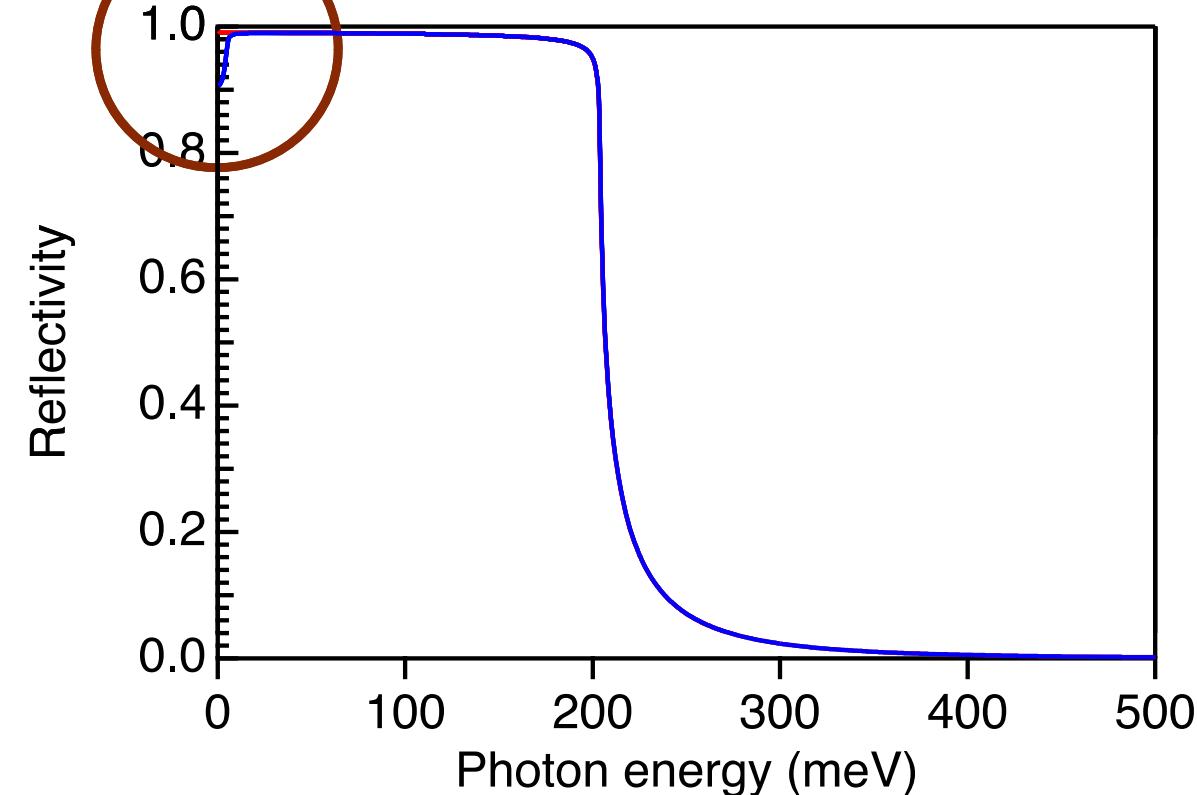
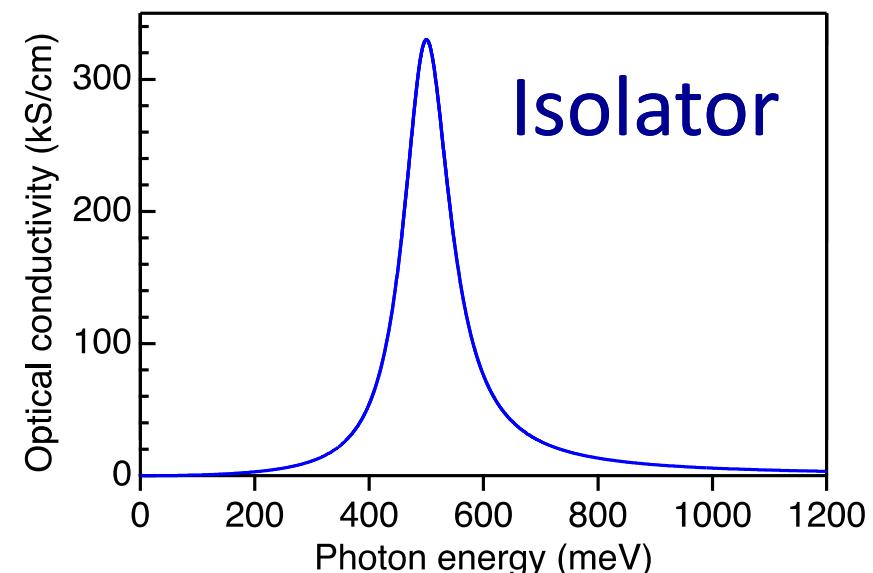
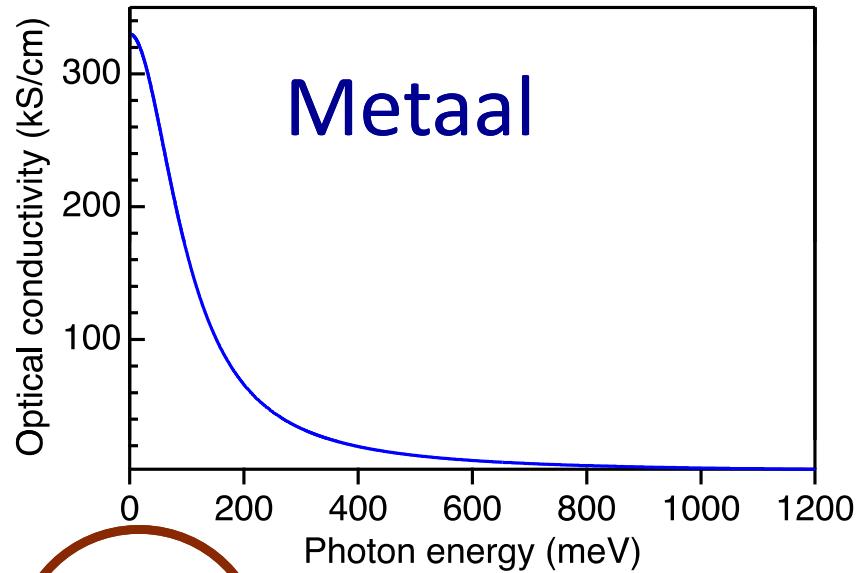
$$\hat{\sigma}(\omega) = \frac{i\omega f^2}{i\omega\Gamma - (\Omega_0^2 - \omega^2)}$$

$$\Omega_0 = \sqrt{\frac{k}{m_e}}$$

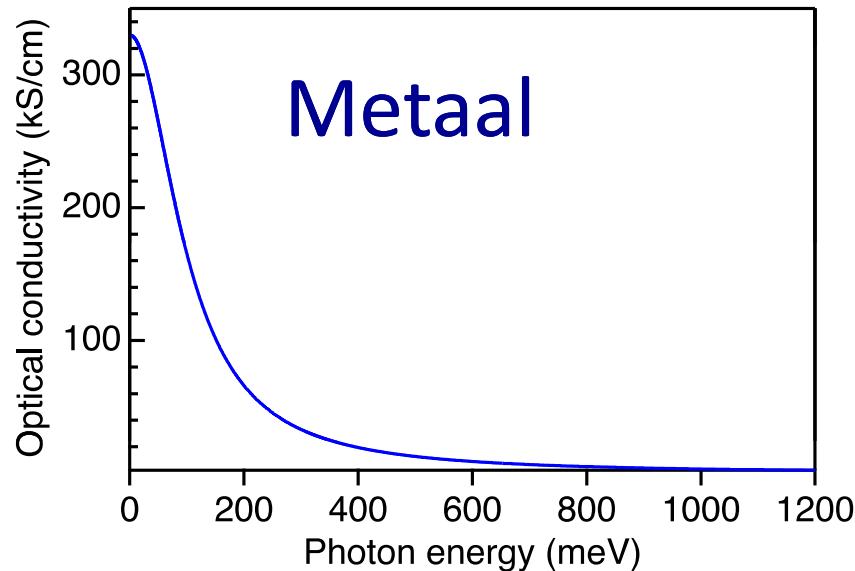




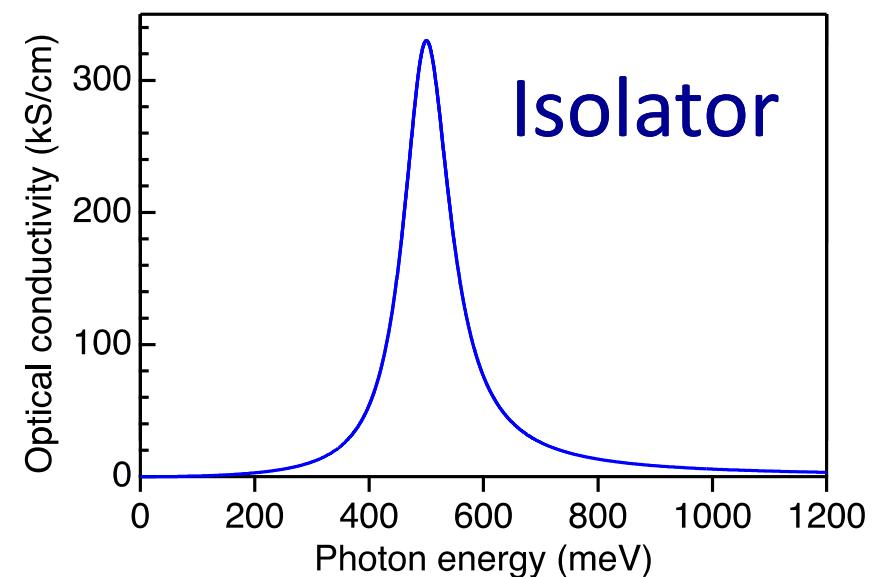
# Probleem



# Probleem



Metaal



Isolator

Golflengte [ $\mu\text{m}$ ]

1000

100

10

1

0.25

THz

FIR

MIR

NIR

VIS

UV

0.5

5

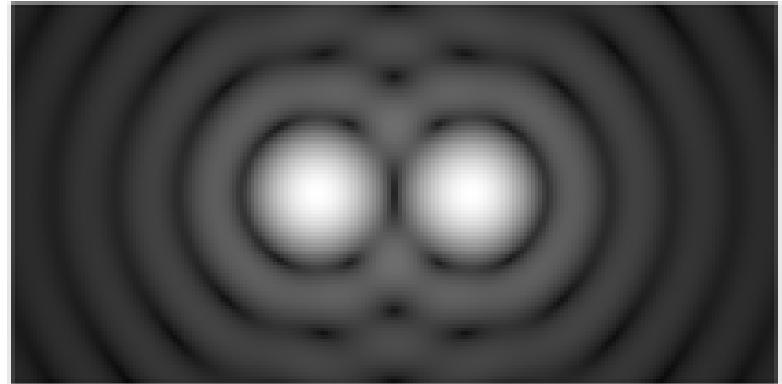
50

500

5000

foton energie [meV]

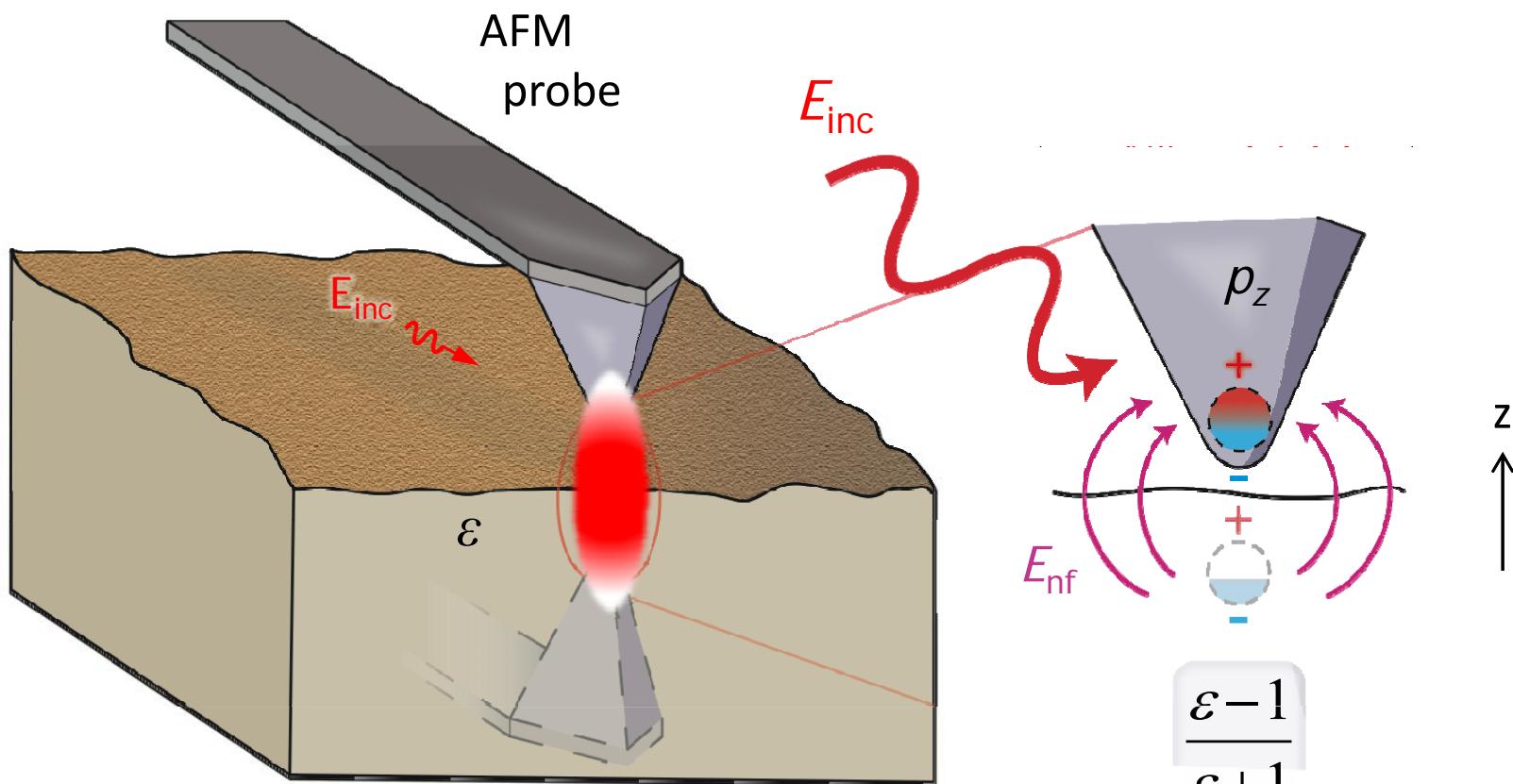
# — De diffractie limiet —



Objecten kleiner dan de golflengte kun je niet onderscheiden!

Het optische verschil tussen metaal en isolator zie je bij  $10\text{-}100 \mu\text{m}$ .

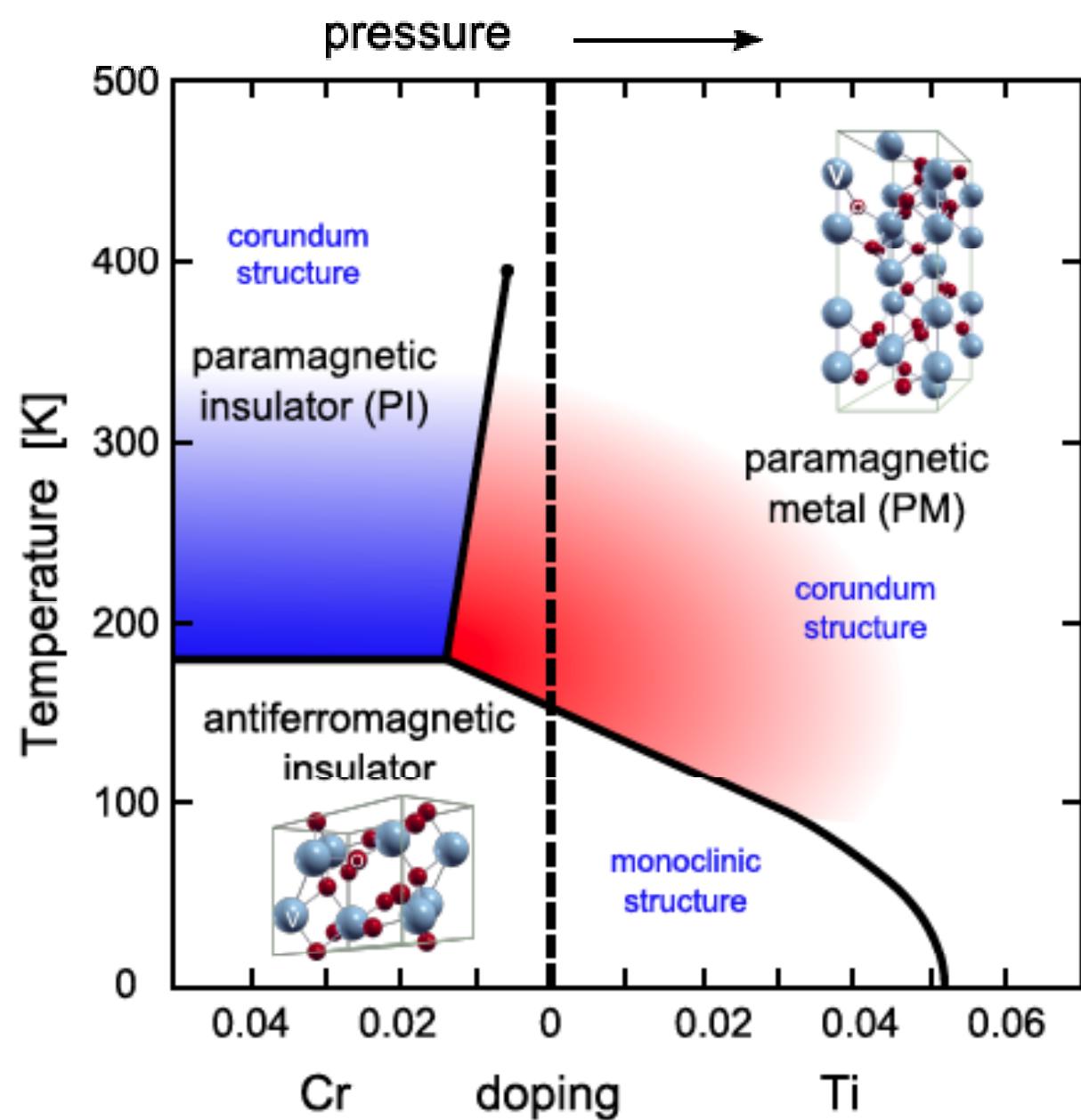
# Nabije veld spectroscopie



- Als je een metalen naald met laser licht bestraalt onstaat een dipool
- Door  $E_{scat}$  te meten terwijl de naald het oppervlak aftast, zie je optisch contrast

$E_{scat}$  bevat lokale informatie over optische geleiding met 20 nm resolution ( $\approx$  straal van AFM punt)

# Metaal-Isolator overgang in $V_2O_3$



Sterk wisselwerkend metaal  
Structurele en magnetische overgangen

Wat drijft de overgang van metaal naar isolator?

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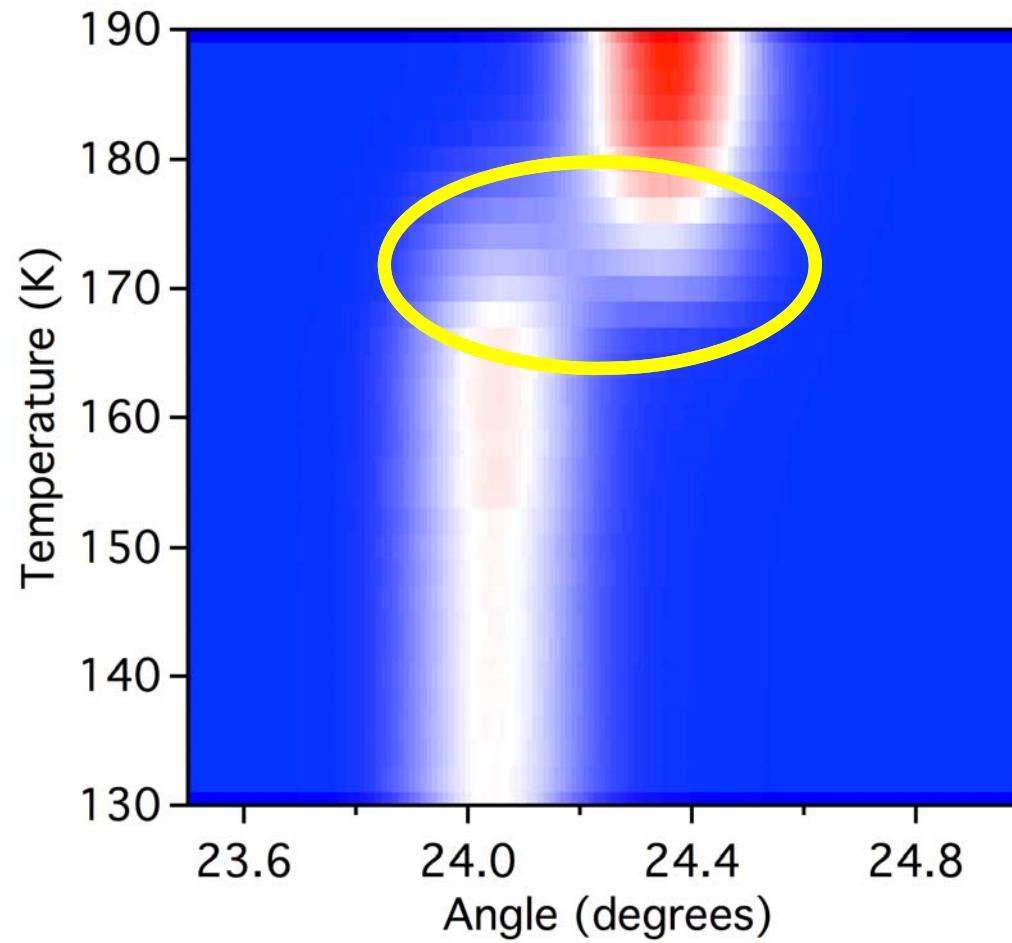
Hansmann et al. Phys. Status Solidi B 250, 1251 (2013)



# V<sub>2</sub>O<sub>3</sub> kristal structuur

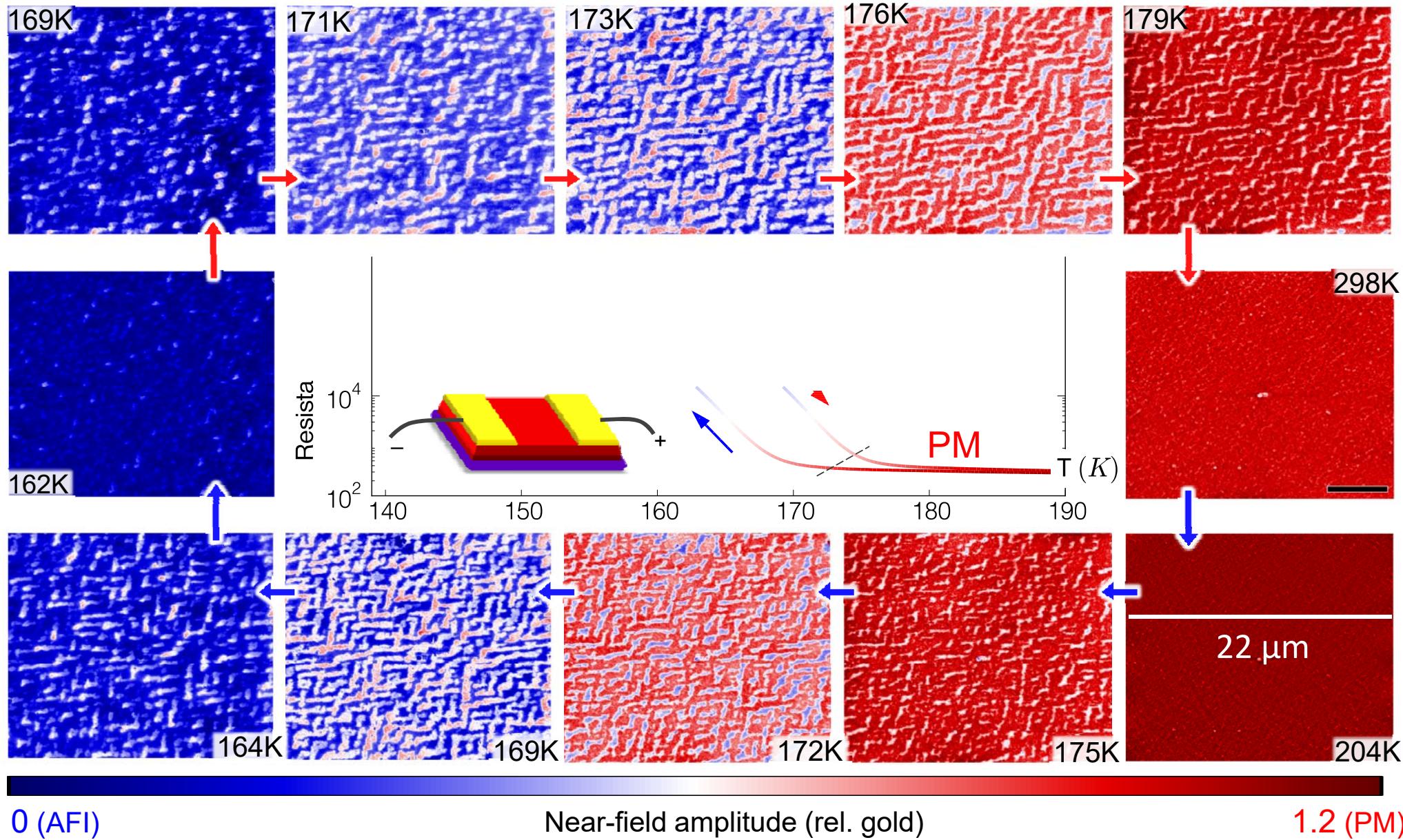
300 nm film V<sub>2</sub>O<sub>3</sub> op saffier

rontgen diffractie: ([110] and [012] peaks)

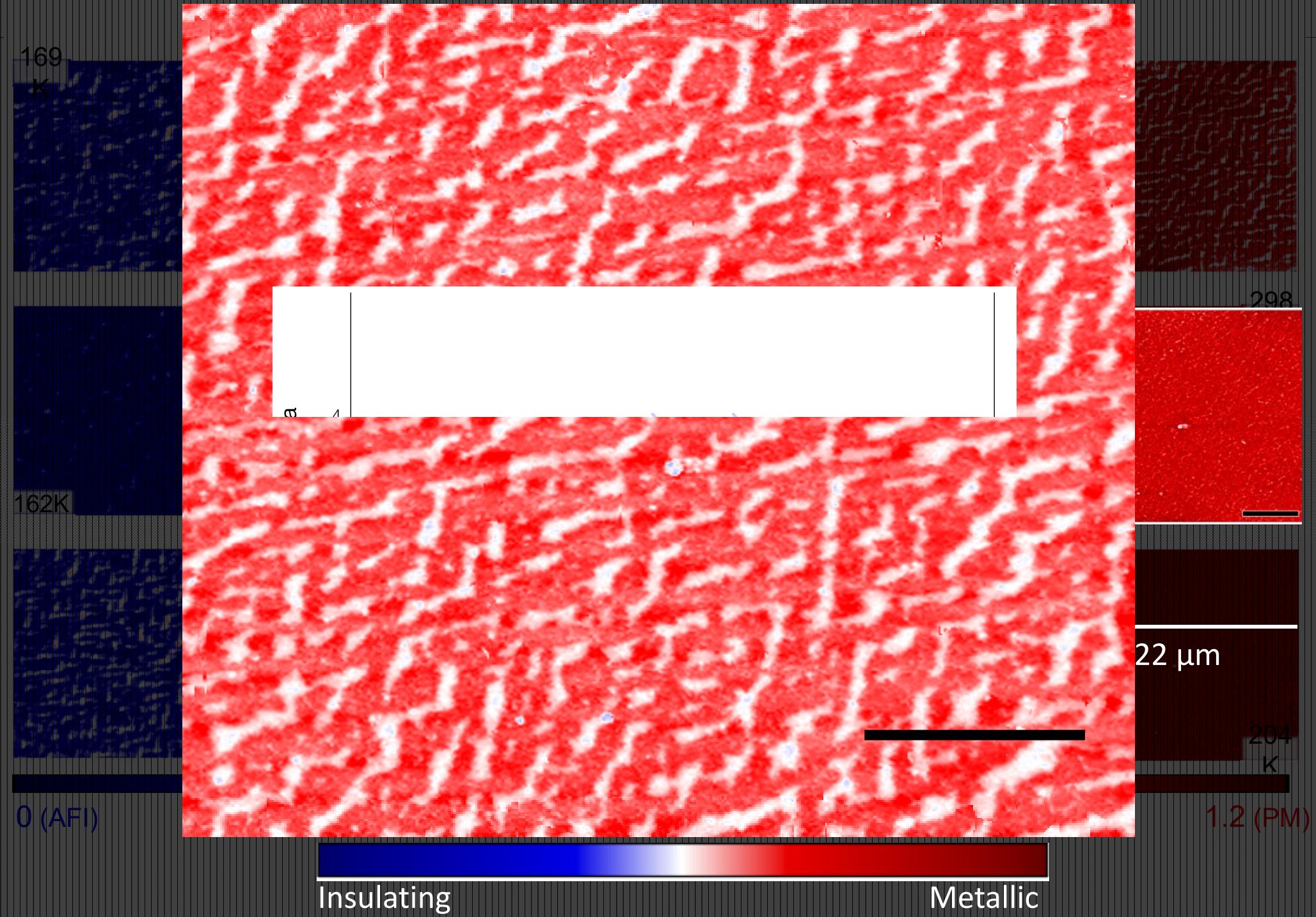


2 structuren bij dezelfde T

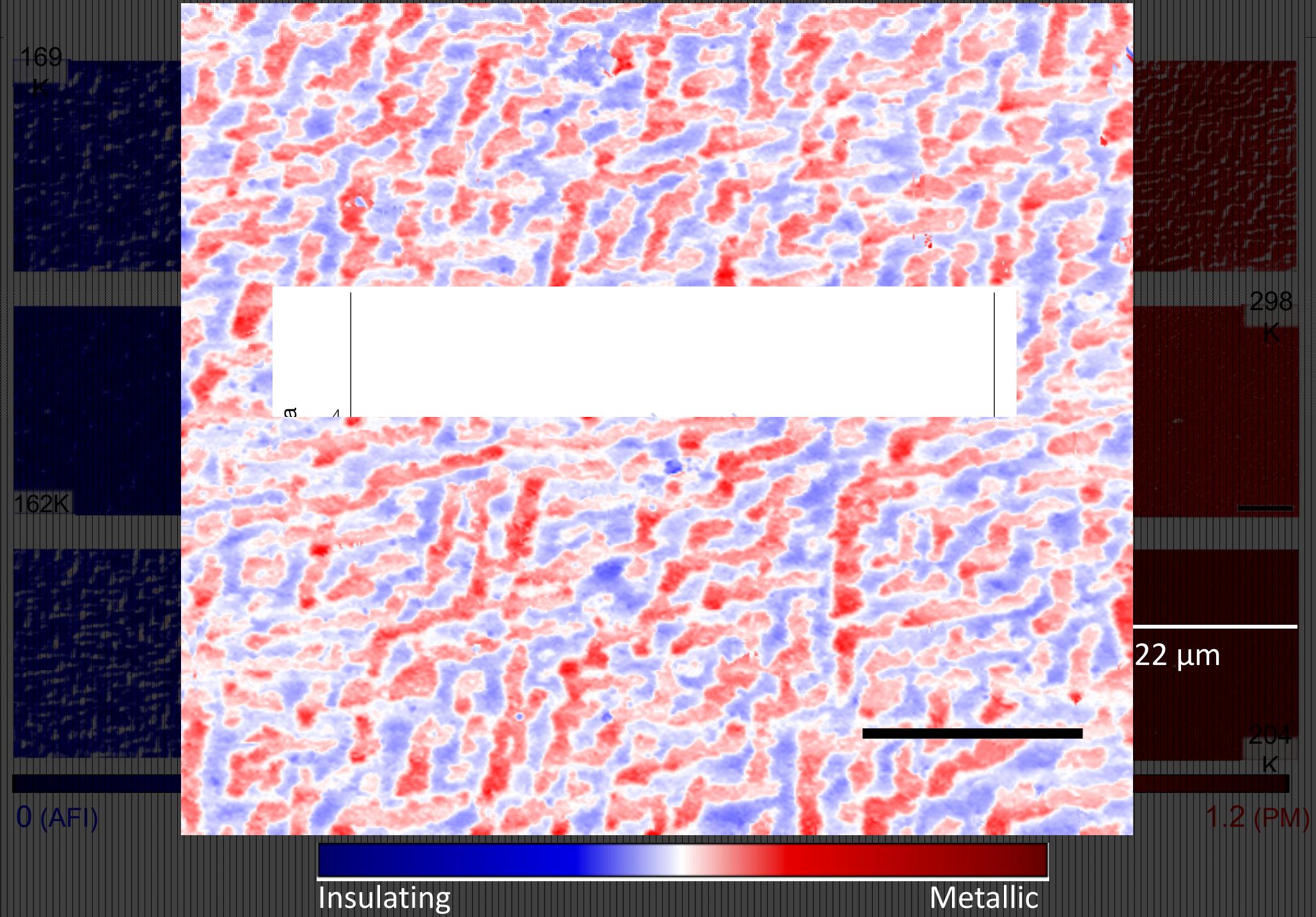
# Near-field maps



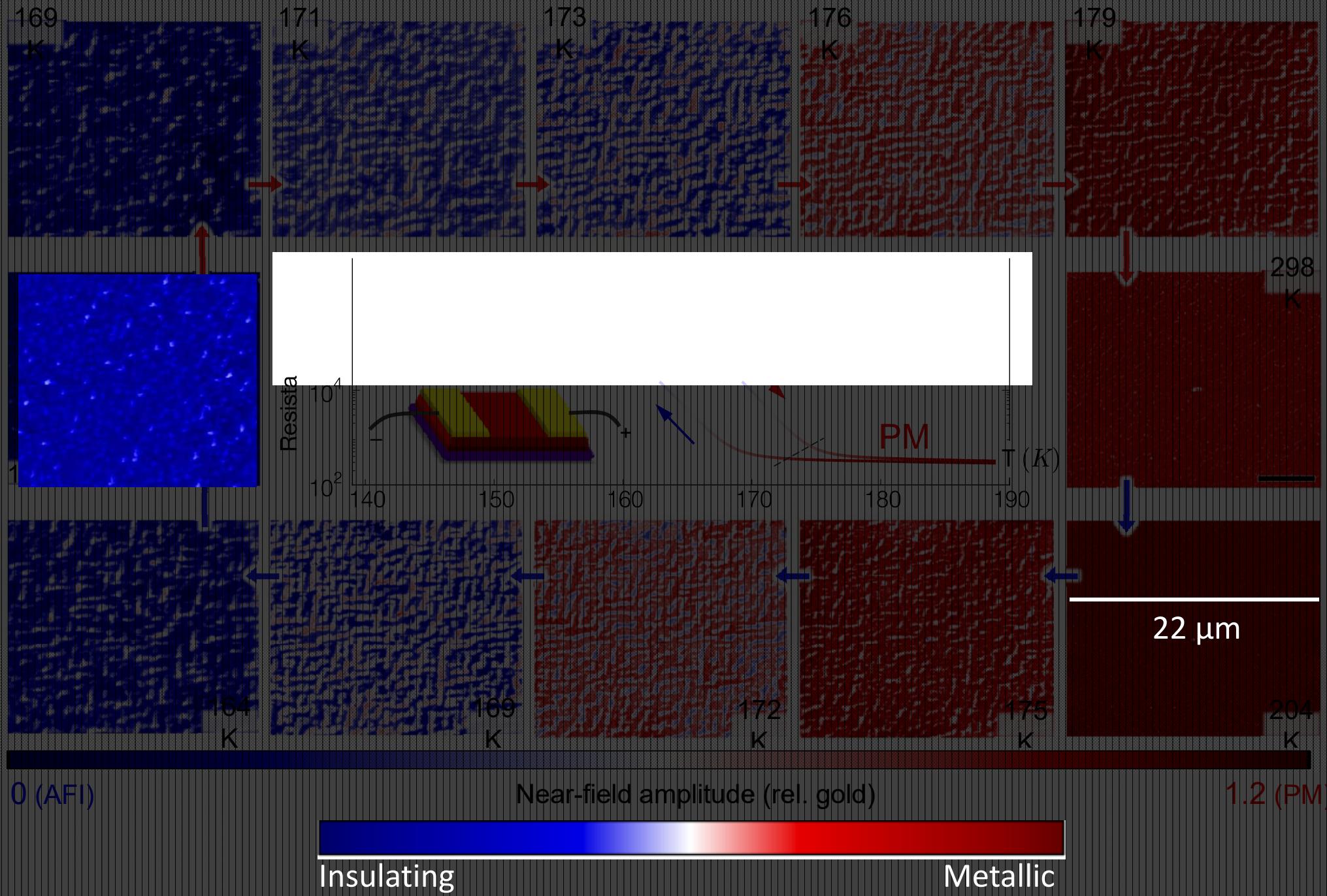
# Near-field maps



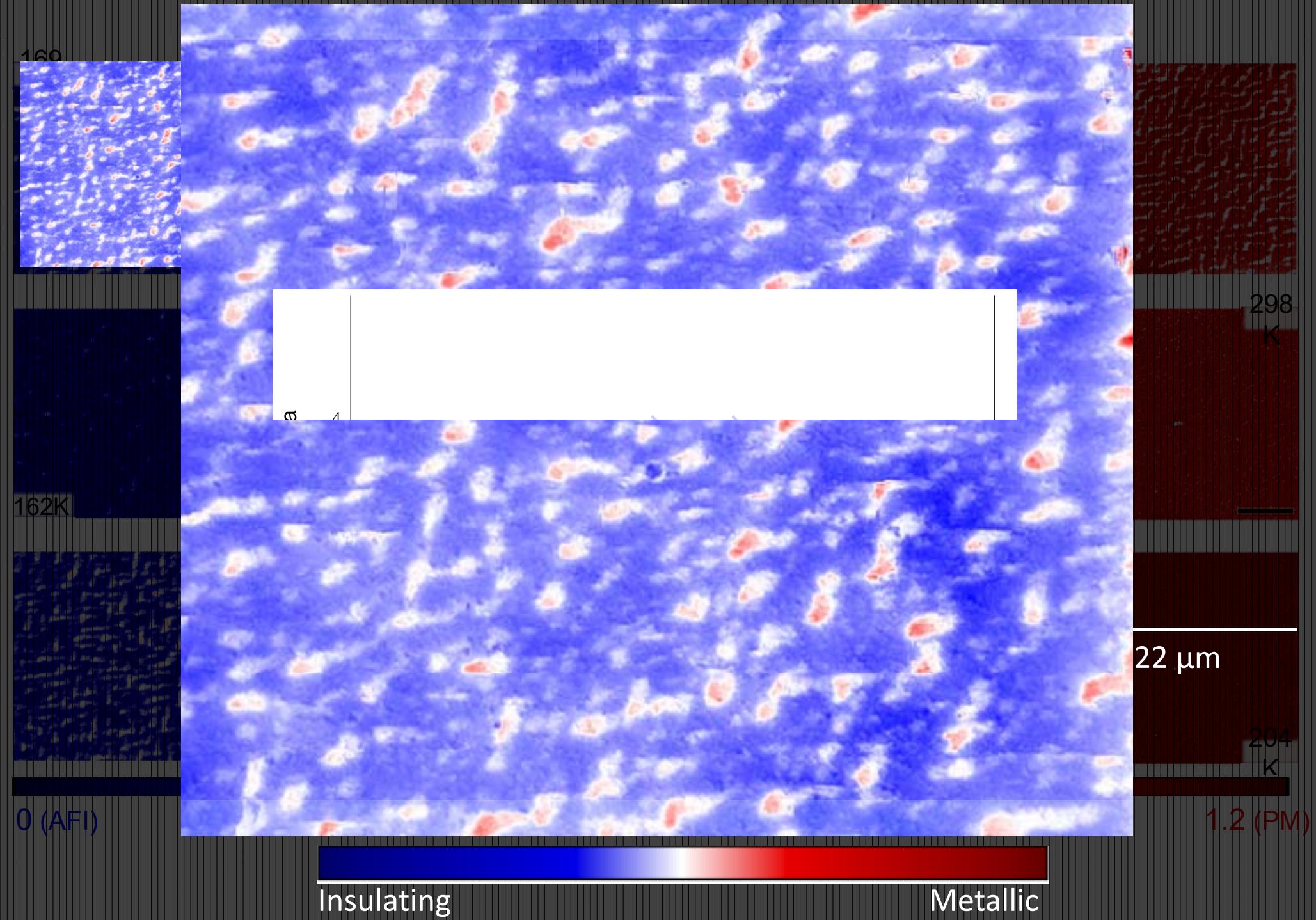
# Near-field maps



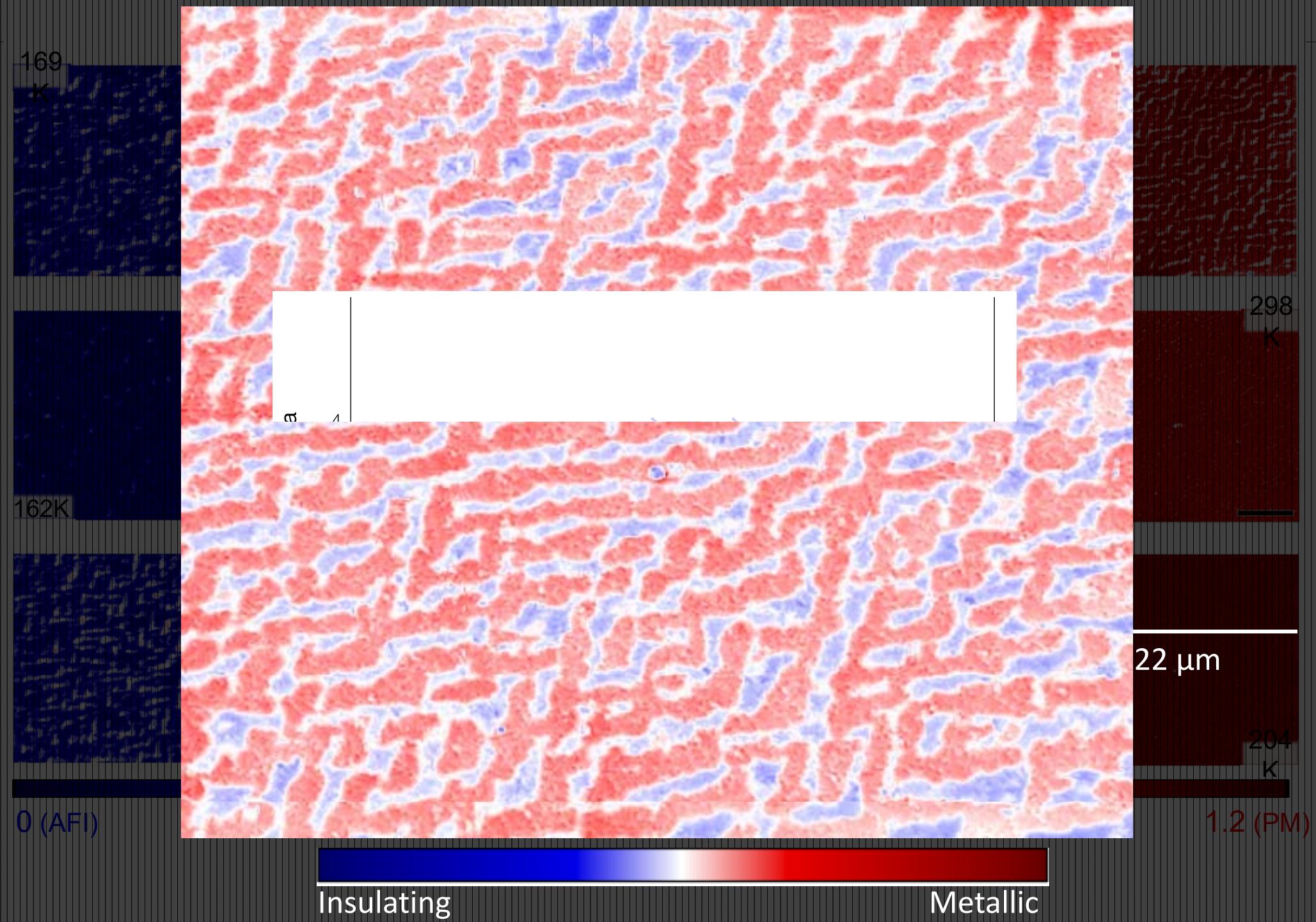
# Near-field maps



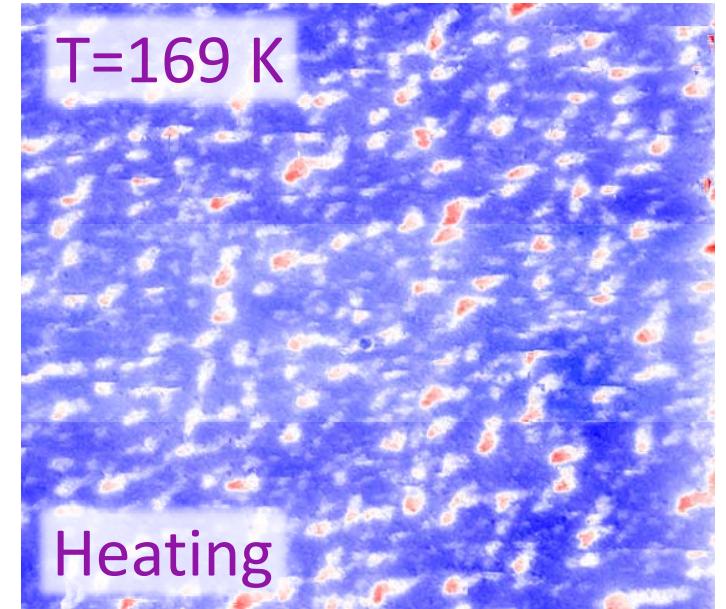
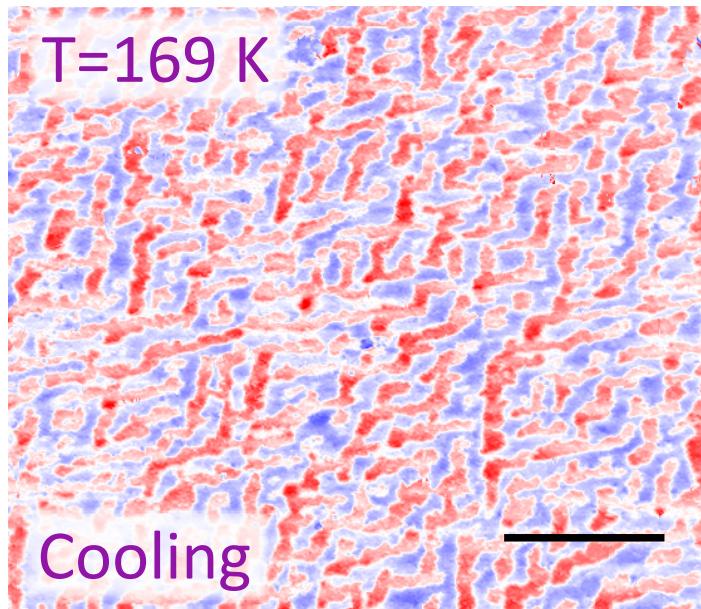
# Near-field maps



# Near-field maps

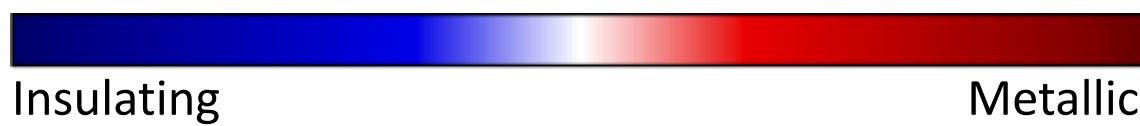


# Two facets of the metal-insulator transition

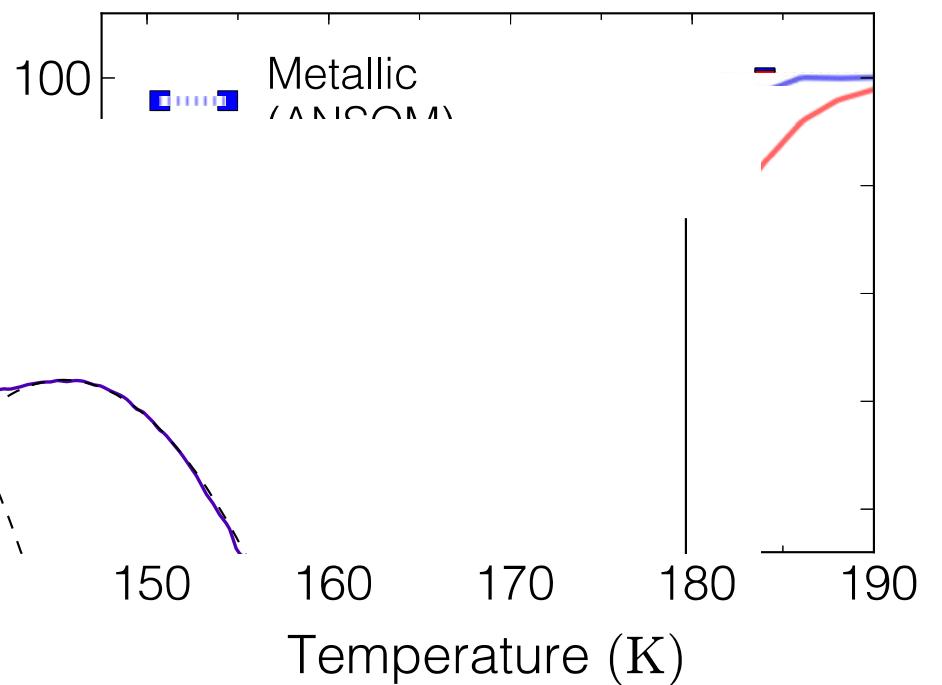
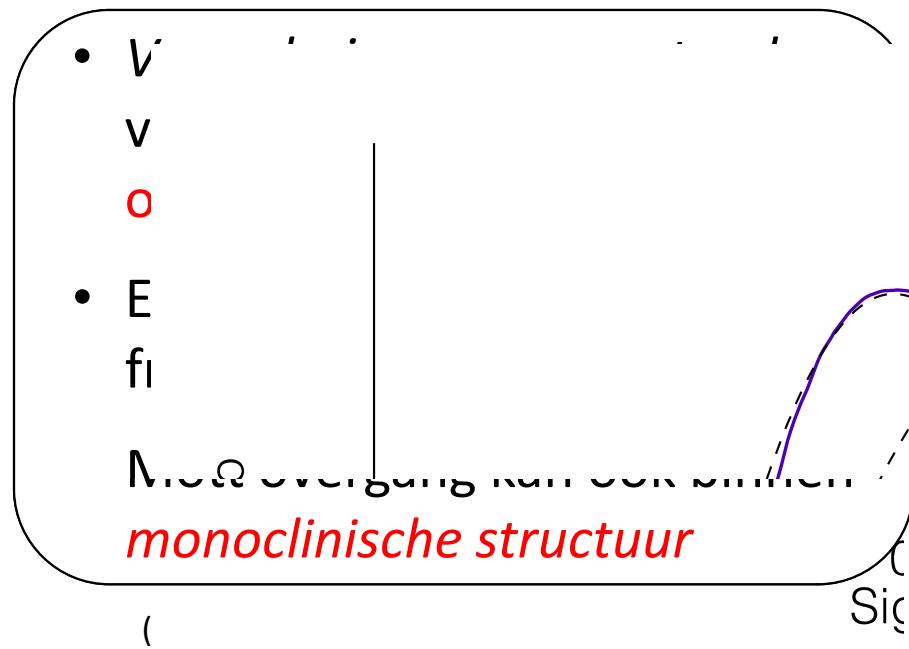
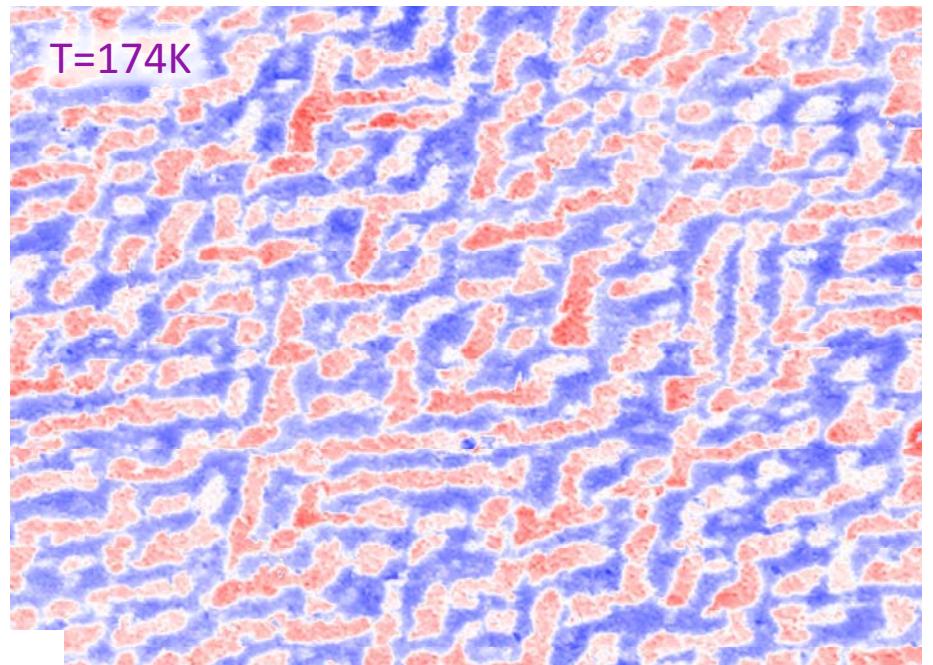
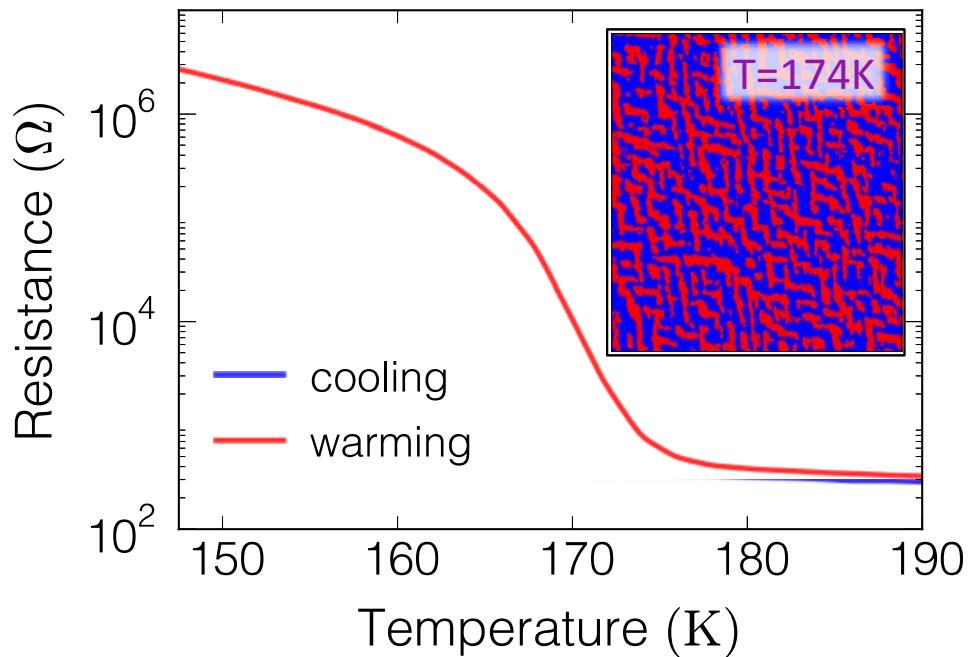


- Conducting stripes
- XRD: transition 75 % completed

- Nucleating conducting puddles
- XRD: transition <5 % completed

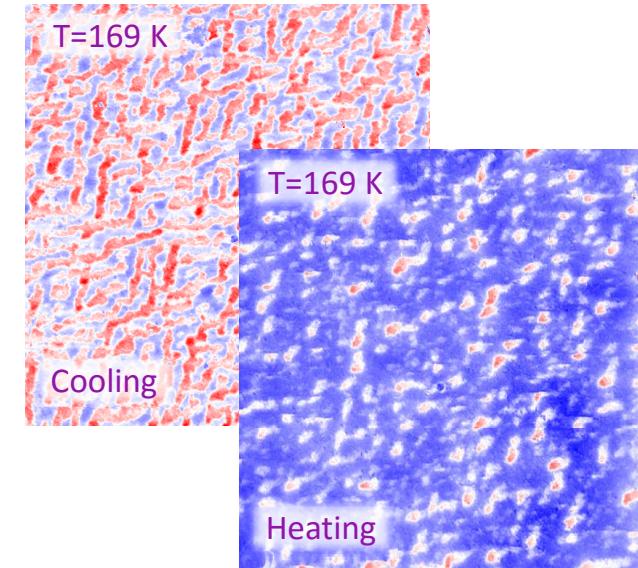


# Percolatie overgang



# Samenvatting

- De verandering van de weerstand wordt gedreven door percolatie.
- De metaal-isolator overgang is niet direct gekoppeld aan de kristal structuur.
- Waarom een gestreept patroon?



## Mogelijk antwoord –

- Koppeling van elektronen aan ‘stress velden’



# Standard Model of FUNDAMENTAL PARTICLES AND INTERACTIONS

The Standard Model summarizes the current knowledge in Particle Physics. It is the quantum theory that includes the theory of strong interactions (quantum chromodynamics or QCD) and the unified theory of weak and electromagnetic interactions (electroweak). Gravity is included on this chart because it is one of the fundamental interactions even though not part of the "Standard Model."

## FERMIONS

matter constituents  
spin = 1/2, 3/2, 5/2, ...

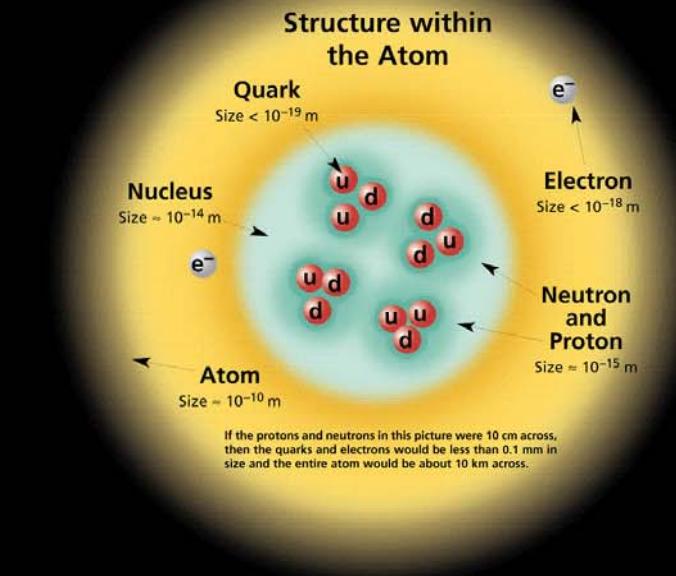
Leptons spin = 1/2		
Flavor	Mass GeV/c <sup>2</sup>	Electric charge
$\nu_e$ electron neutrino	$<1 \times 10^{-8}$	0
e electron	0.000511	-1
$\nu_\mu$ muon neutrino	$<0.0002$	0
$\mu$ muon	0.106	-1
$\nu_\tau$ tau neutrino	$<0.02$	0
$\tau$ tau	1.7771	-1

Quarks spin = 1/2		
Flavor	Approx. Mass GeV/c <sup>2</sup>	Electric charge
u up	0.003	2/3
d down	0.006	-1/3
c charm	1.3	2/3
s strange	0.1	-1/3
t top	175	2/3
b bottom	4.3	-1/3

Spin is the intrinsic angular momentum of particles. Spin is given in units of  $\hbar$ , which is the quantum unit of angular momentum, where  $\hbar = h/2\pi = 6.58 \times 10^{-25}$  GeV s =  $1.05 \times 10^{-34}$  J s.

Electric charges are given in units of the proton's charge. In SI units the electric charge of the proton is  $1.60 \times 10^{-19}$  coulombs.

The energy unit of particle physics is the electronvolt (eV), the energy gained by one electron in crossing a potential difference of one volt. Masses are given in GeV/c<sup>2</sup> (remember  $E = mc^2$ ), where 1 GeV =  $10^9$  eV =  $1.60 \times 10^{-10}$  joule. The mass of the proton is 0.938 GeV/c<sup>2</sup> =  $1.67 \times 10^{-27}$  kg.



## BOSONS

force carriers  
spin = 0, 1, 2, ...

Unified Electroweak spin = 1		
Name	Mass GeV/c <sup>2</sup>	Electric charge
$\gamma$ photon	0	0
$W^-$	80.4	-1
$W^+$	80.4	+1
$Z^0$	91.187	0

Strong (color) spin = 1		
Name	Mass GeV/c <sup>2</sup>	Electric charge
g gluon	0	0

**Color Charge**  
Each quark carries one of three types of "strong charge," also called "color charge." These charges have nothing to do with the colors of visible light. There are eight possible types of color charge for gluons. Just as electrically-charged particles interact by exchanging photons, in strong interactions color-charged particles interact by exchanging gluons. Leptons, photons, and  $W$  and  $Z$  bosons have no strong interactions and hence no color charge.

### Quarks Confined in Mesons and Baryons

One cannot isolate quarks and gluons; they are confined in color-neutral particles called **hadrons**. This confinement (binding) results from multiple exchanges of gluons among the color-charged constituents. As color-charged particles (quarks and gluons) move apart, the energy in the color-force field between them increases. This energy eventually is converted into additional quark-antiquark pairs (see figure below). The quarks and antiquarks then combine into hadrons; these are the particles seen to emerge. Two types of hadrons have been observed in nature: **mesons**  $q\bar{q}$  and **baryons**  $qqq$ .

### Residual Strong Interaction

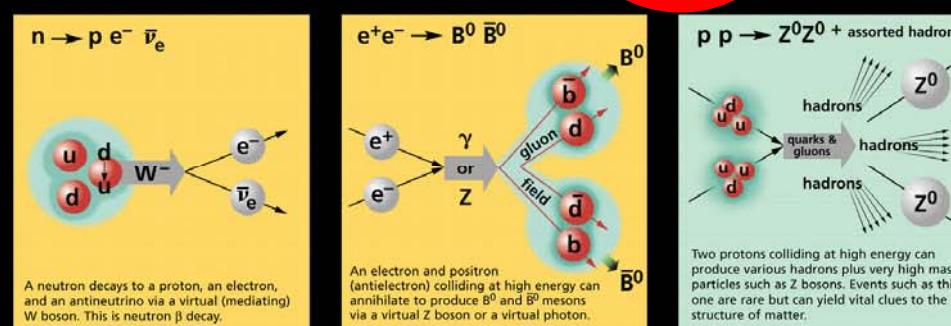
The strong binding of color-neutral protons and neutrons to form nuclei is due to residual strong interactions between their color-charged constituents. It is similar to the residual electrical interaction that binds electrically neutral atoms to form molecules. It can also be viewed as the exchange of mesons between the hadrons.

## PROPERTIES OF THE INTERACTIONS

Baryons $qqq$ and Antibaryons $\bar{q}\bar{q}\bar{q}$					
Baryons are fermionic hadrons. There are about 120 types of baryons.					
Symbol	Name	Quark content	Electric charge	Mass GeV/c <sup>2</sup>	Spin
p	proton	uud	1	0.938	1/2
$\bar{p}$	anti-proton	$\bar{u}\bar{u}\bar{d}$	-1	0.938	1/2
n	neutron	udd	0	0.940	1/2
$\Lambda$	lambda	uds	0	1.116	1/2
$\Omega^-$	omega	sss	-1	1.672	3/2

Property	Interaction		Gravitational	Weak (Electroweak)	Electromagnetic	Fundamental	Residual
	Acts on:	Particles experiencing:		Flavor	Electric Charge		
		All	Quarks, Lepton	Electrically charged	Quarks, Gluons	Hadrons	
	Particles mediating:	Graviton (not yet observed)	$W^+$ $W^-$ $Z$	$\gamma$	Gluons	Mesons	
	Strength relative to electromagnetism	$10^{-18}$ m for two u quarks at: $3 \times 10^{-17}$ m	$10^{-41}$	0.8	1	25	
		for two protons in nucleus	$10^{-41}$	$10^{-4}$	1	60	Not applicable to hadrons
			$10^{-36}$	$10^{-7}$	1	20	

Mesons $q\bar{q}$					
Mesons are bosonic hadrons. There are about 140 types of mesons.					
Symbol	Name	Quark content	Electric charge	Mass GeV/c <sup>2</sup>	Spin
$\pi^+$	pion	$u\bar{d}$	+1	0.140	0
$K^-$	kaon	$s\bar{u}$	-1	0.494	0
$\rho^+$	rho	$u\bar{d}$	+1	0.770	1
$B^0$	B-zero	$d\bar{b}$	0	5.279	0
$\eta_c$	eta-c	$c\bar{c}$	0	2.980	0



The Particle Adventure  
Visit the award-winning web feature *The Particle Adventure* at <http://ParticleAdventure.org>

This chart has been made possible by the generous support of:

U.S. Department of Energy  
U.S. National Science Foundation  
Lawrence Berkeley National Laboratory  
Stanford Linear Accelerator Center  
American Physical Society, Division of Particles and Fields  
**BURLE** INDUSTRIES, INC.

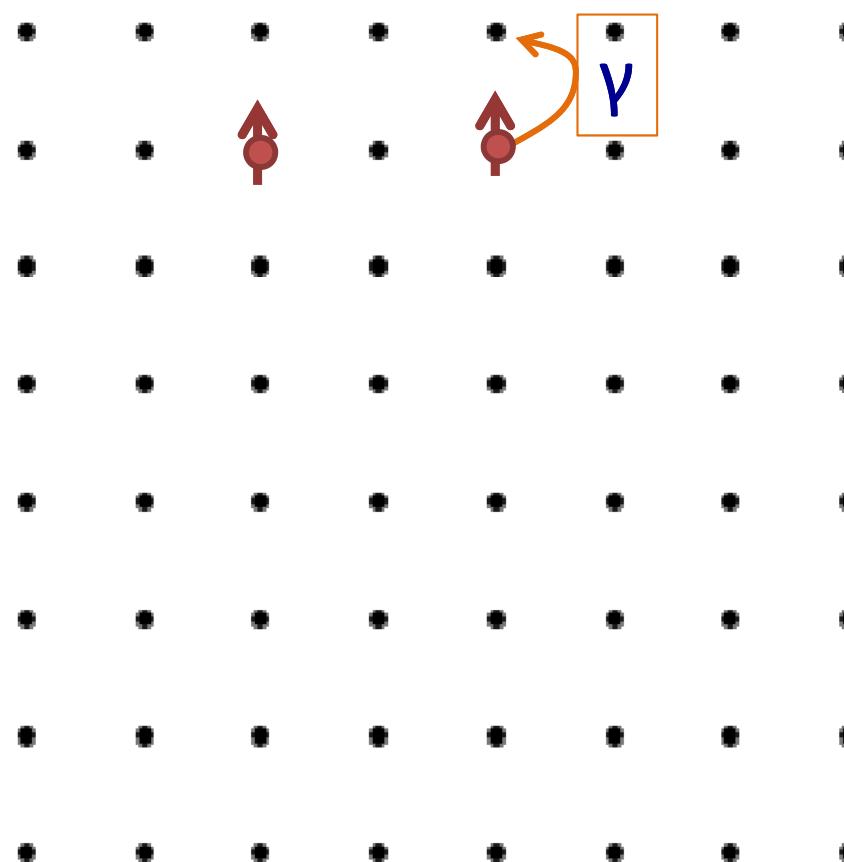
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<http://CPEPweb.org>

### Figures

These diagrams are an artist's conception of physical processes. They are not exact and have no meaningful scale. Green shaded areas represent the cloud of gluons or the gluon field, and red lines the quark paths.

# The Hubbard model

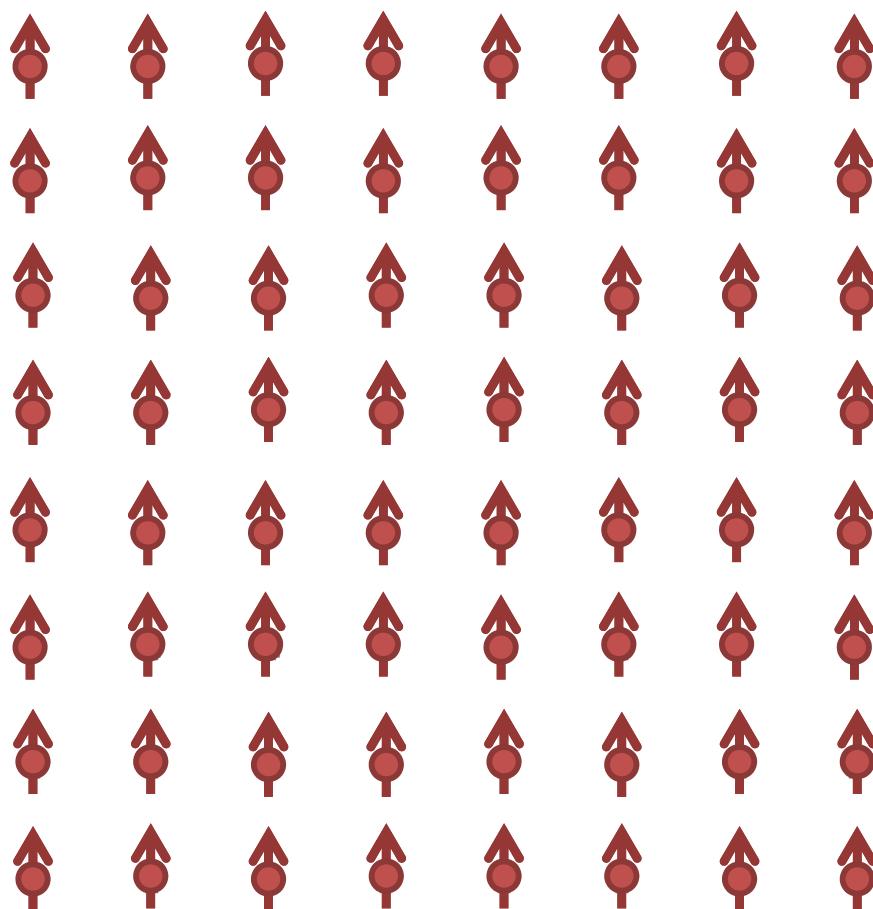
- Neem een rooster van atomen.



# The Hubbard model

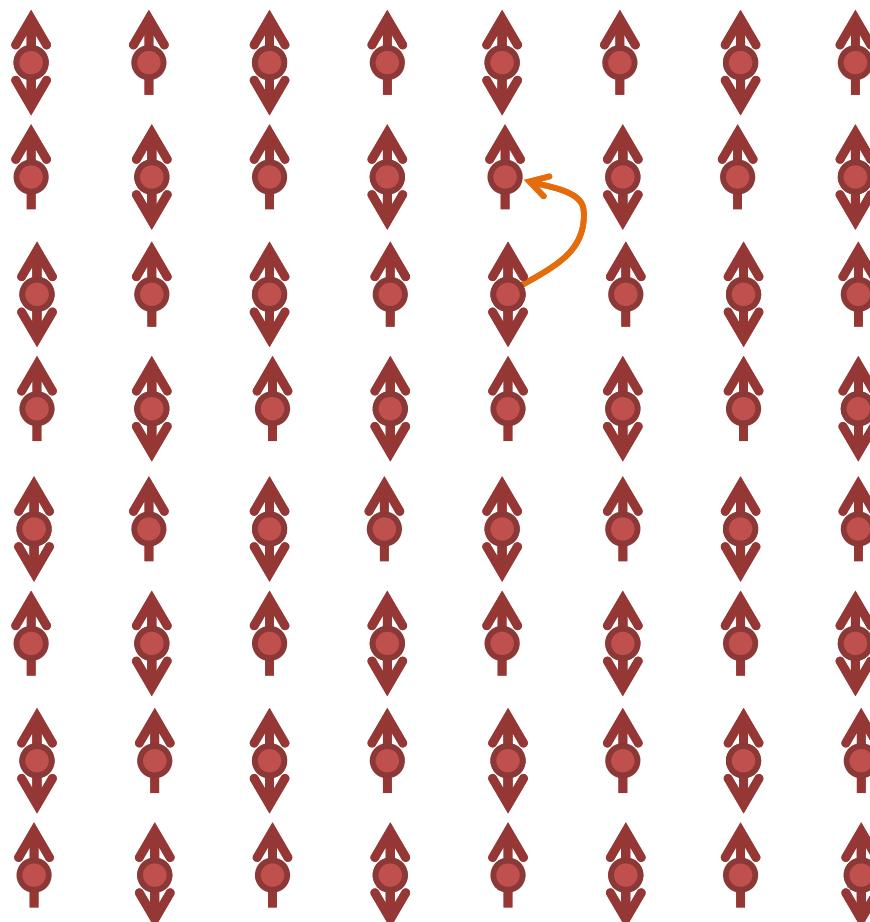


Neem een rooster van atomen.



# The Hubbard model

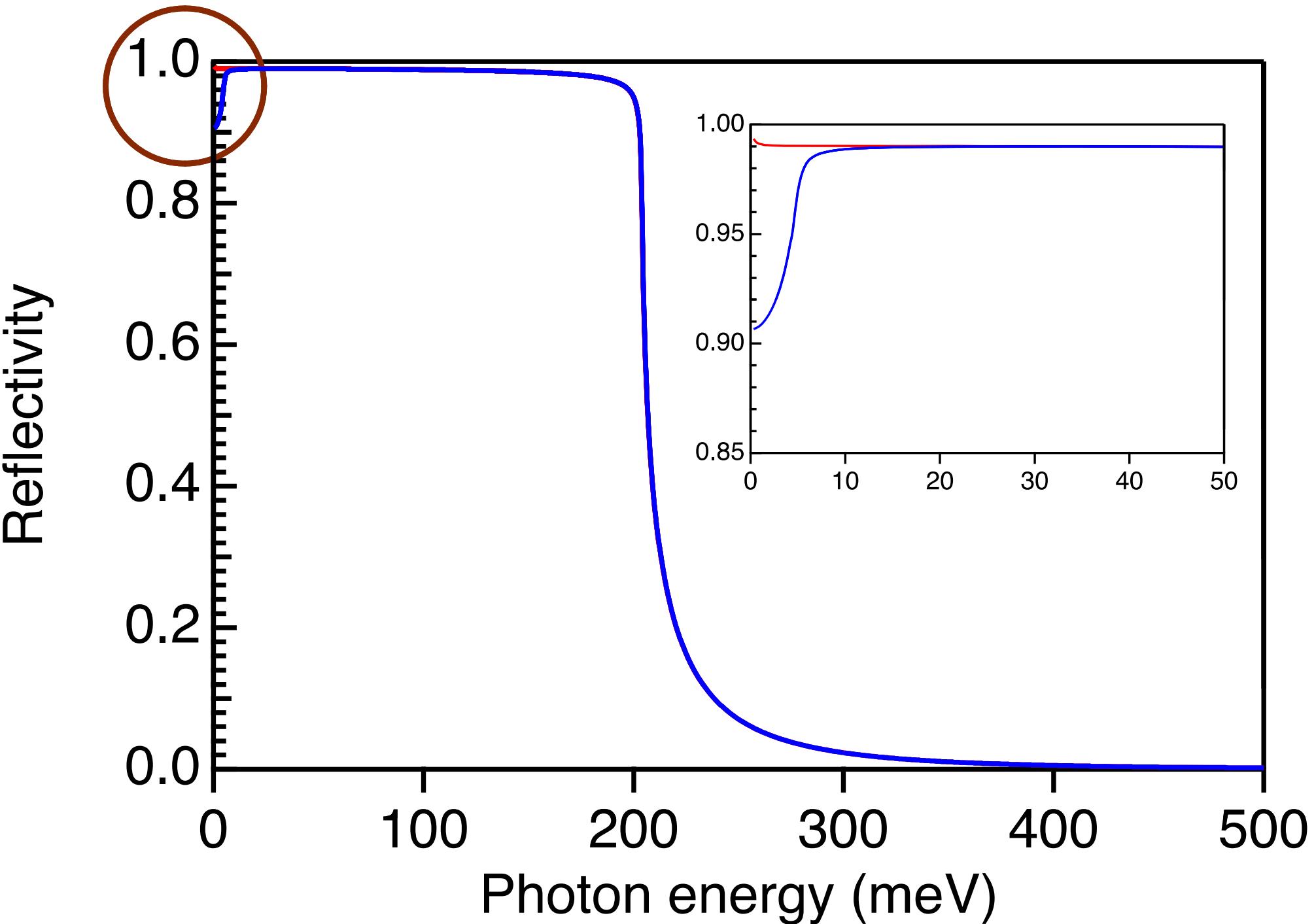
- Neem een rooster van atomen.



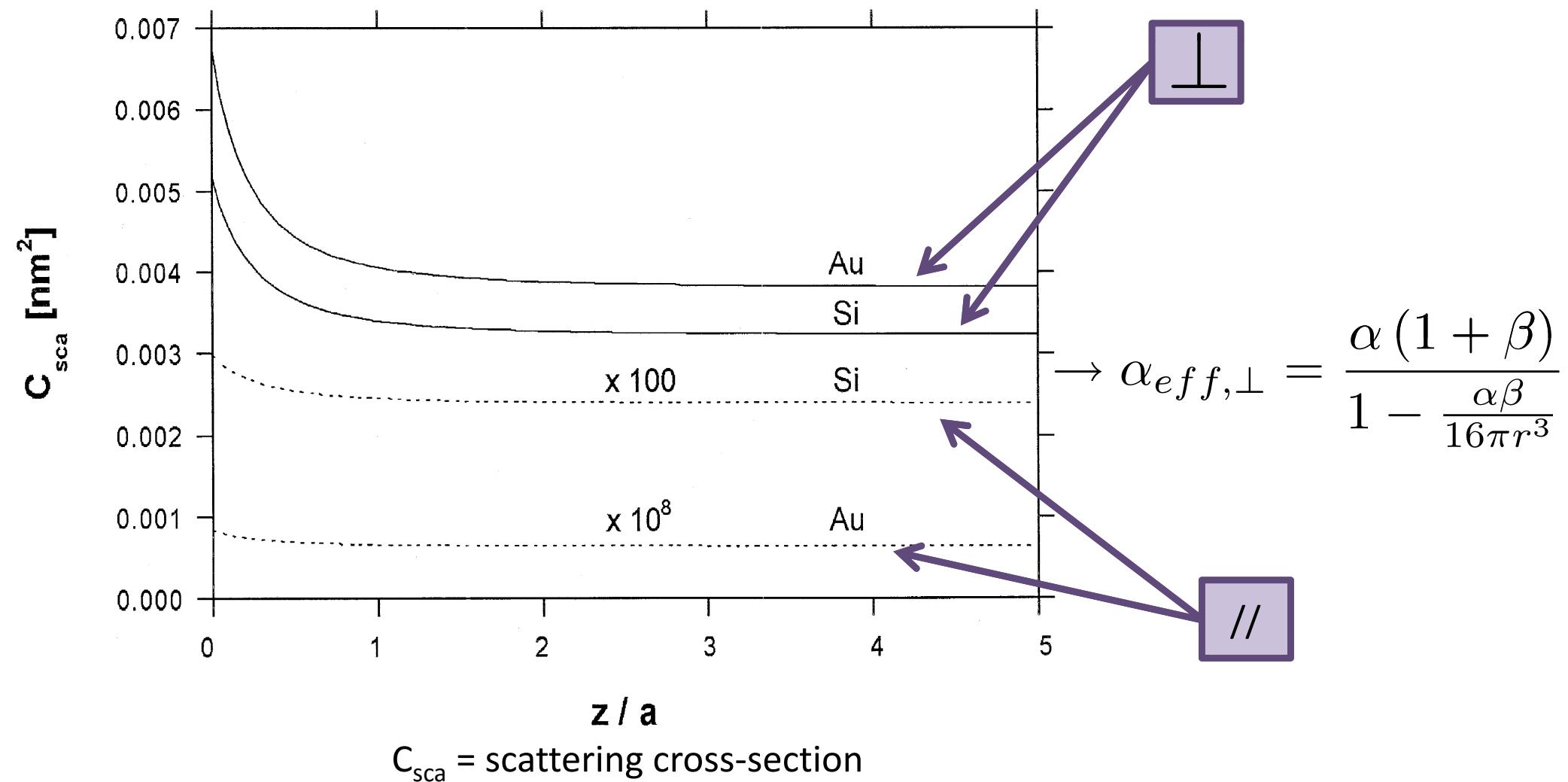
Mott-Hubbard  
isolator

- Met anti-parallelle spins winnen ze  $E_{\text{kin}}$

# De reflectiviteit -



# Near field enhancement

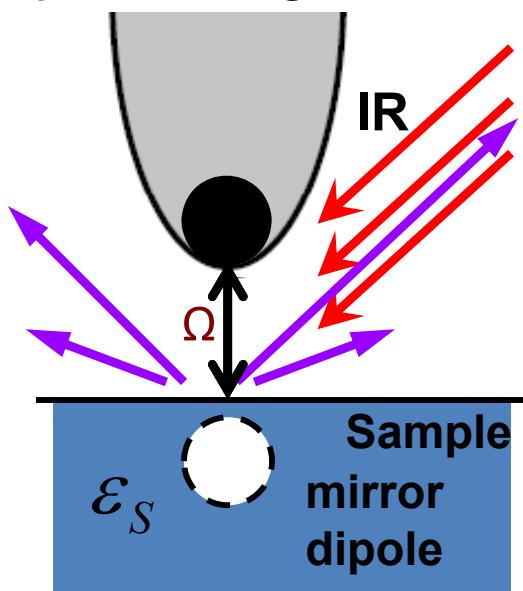


$C_{sca}$  = scattering cross-section

- Strong enhancement when tip approaches sample
- Enhancement for *perpendicular* polarization

# Detection scheme

$$E_s = E_{BG} + E_{NF}$$



$$I \propto |E_s|^2 = E_s E_s^*$$

$$\propto |E_{BG}|^2 + |E_{NF}|^2 + E_{BG}E_{NF}^* + E_{BG}^*E_{NF}$$

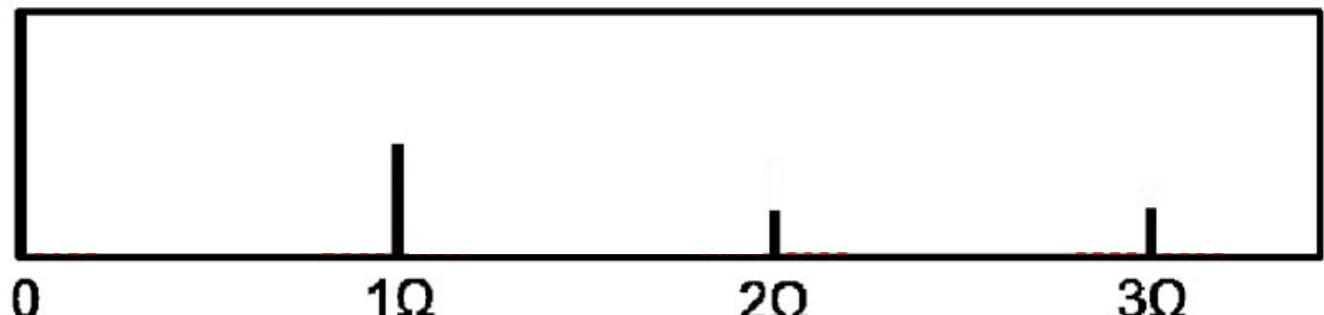


Modulate AFM tip at  $\Omega$

$$E_s = \sum_n \tau_n \exp(in\Omega t) \quad | \quad \tau_n = s_n e^{i\phi_n} + s_{b,n} e^{i\phi_{b,n}}$$

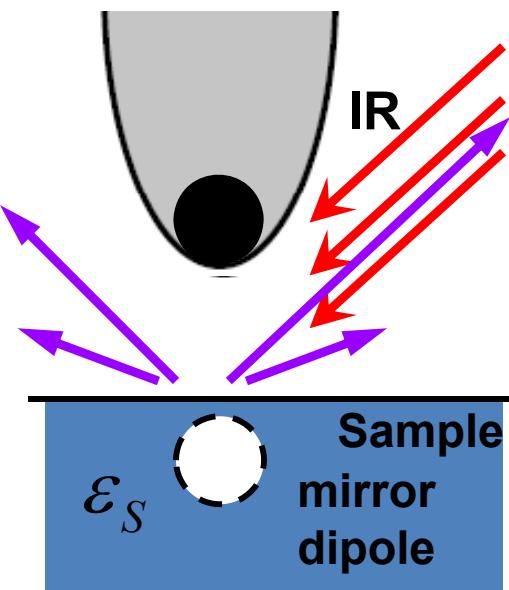
$$I \propto \sum_{n,n'} \tau_n \tau_{n'}^* \exp(i(n-n')\Omega t)$$

$$n^{th} \text{ harmonic} \rightarrow 2\kappa s_{b,0} s_n \cos(\phi_{b,0} - \phi_n)$$

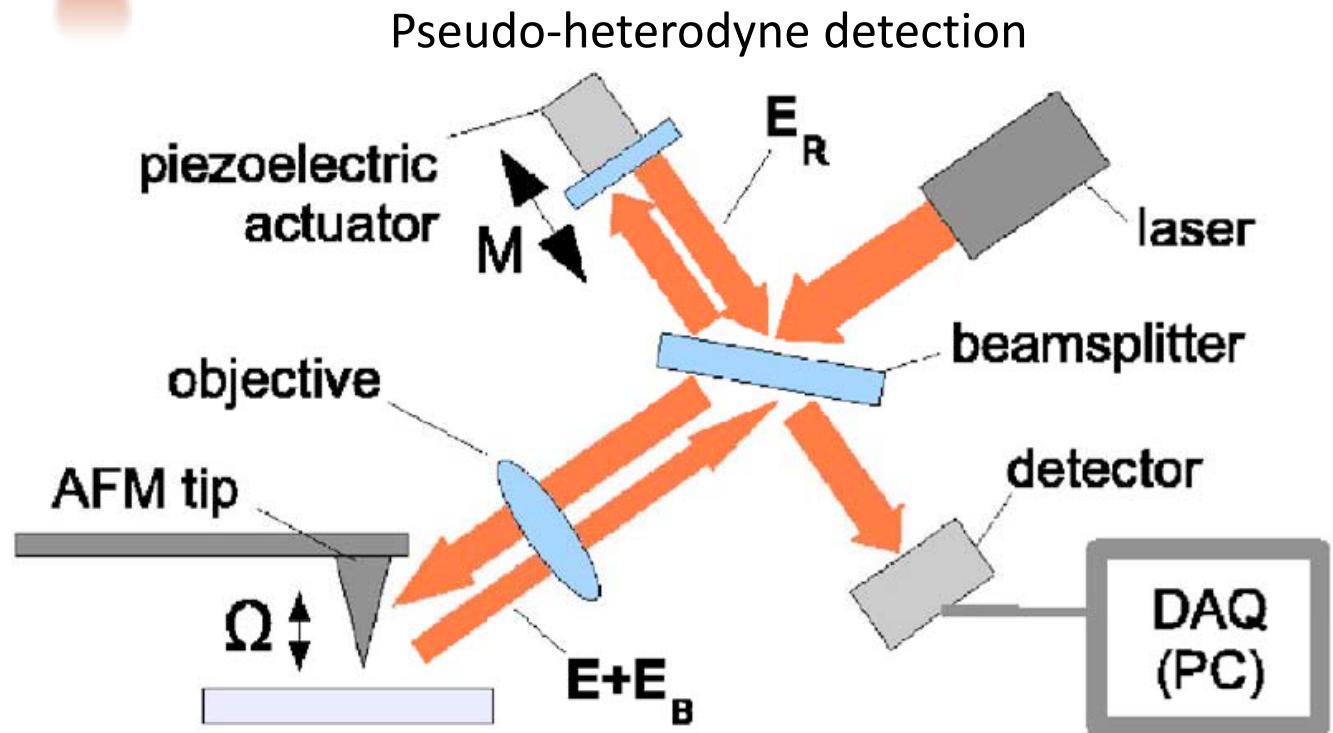


# Interferometric detection

$$E_s = E_{BG} + E_{NF}$$

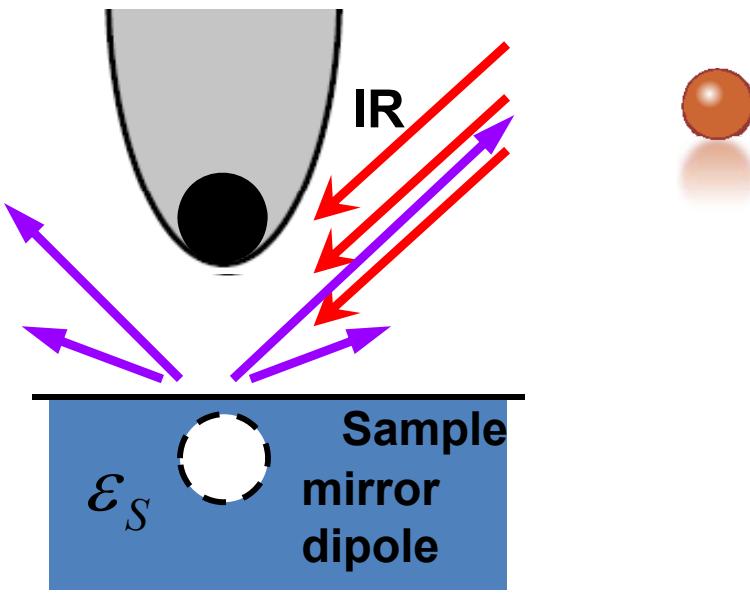


How to remove background?



# Interferometric detection

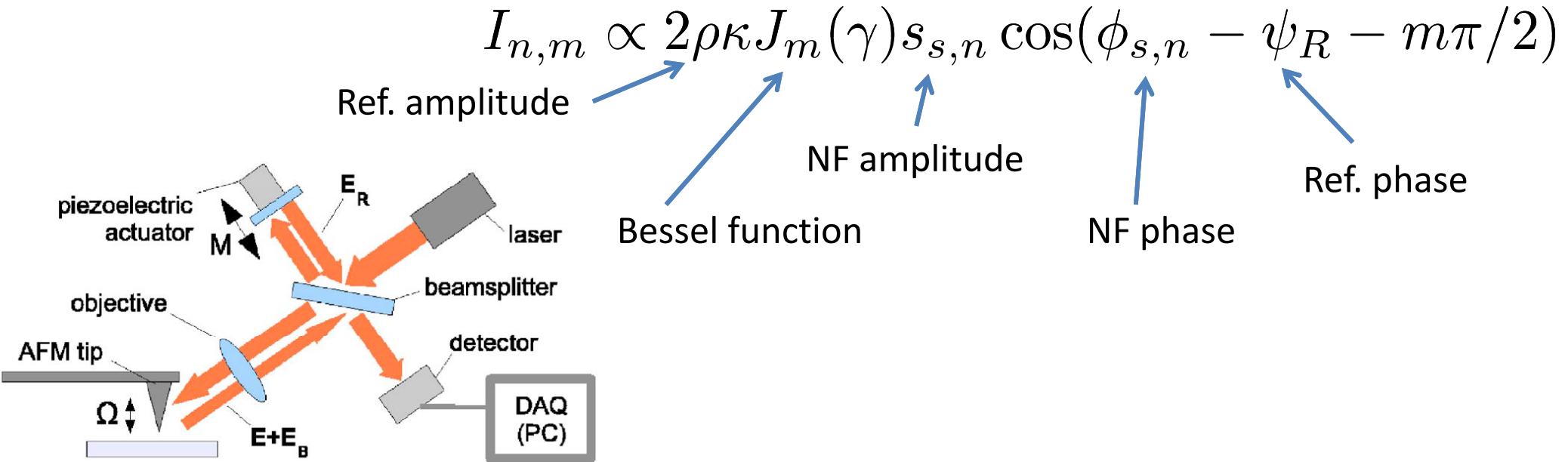
$$E_s = E_{BG} + E_{NF}$$



How to remove background?

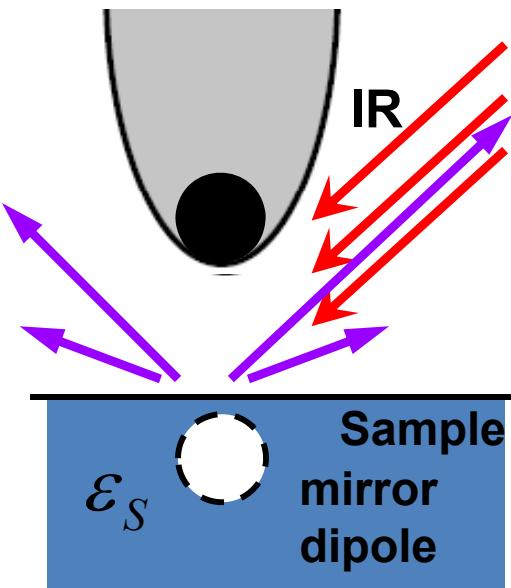
Pseudo-heterodyne detection

$$\begin{aligned} E_R &= \rho \exp(i\gamma \sin(Mt) + i\phi_R) \\ &= \sum_m \rho_m \exp(imMt) \\ \rho_m &= \rho J_m(\gamma) \exp(i\phi_R + im\pi/2) \end{aligned}$$

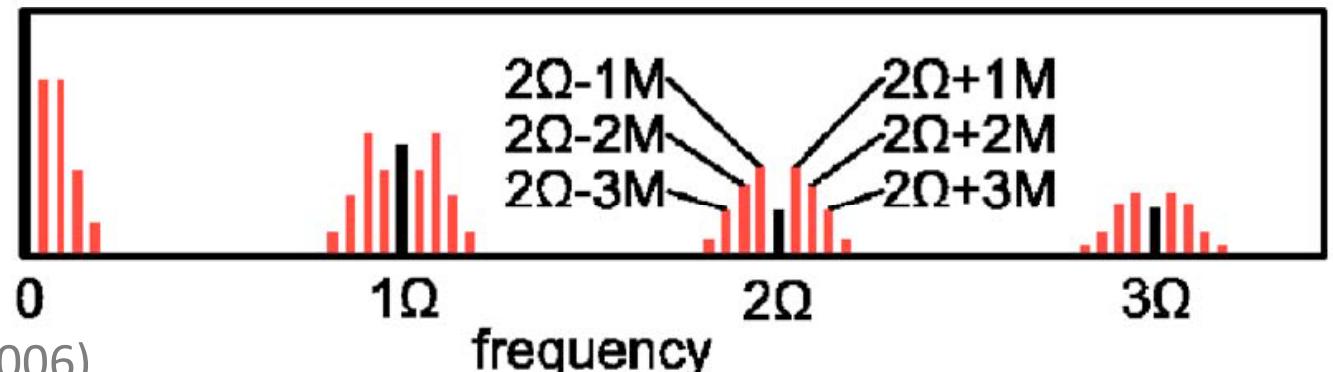
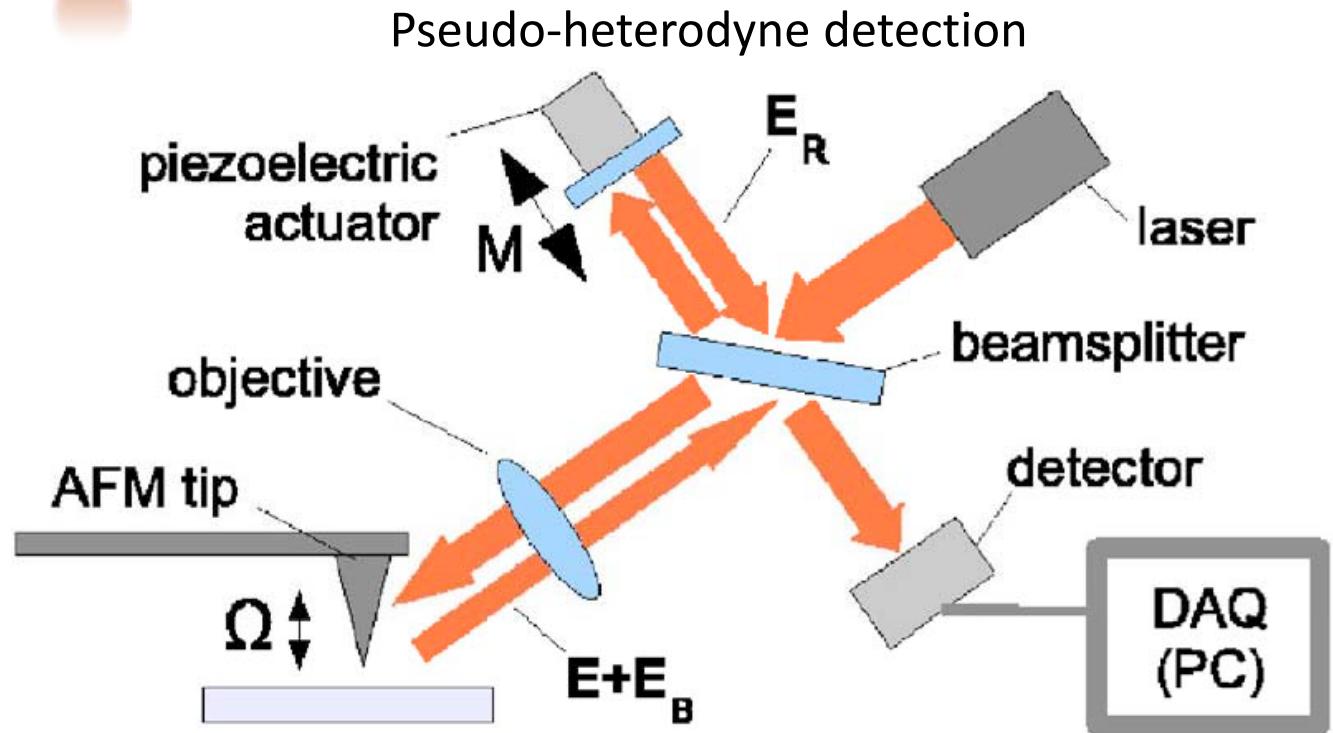


# Interferometric detection

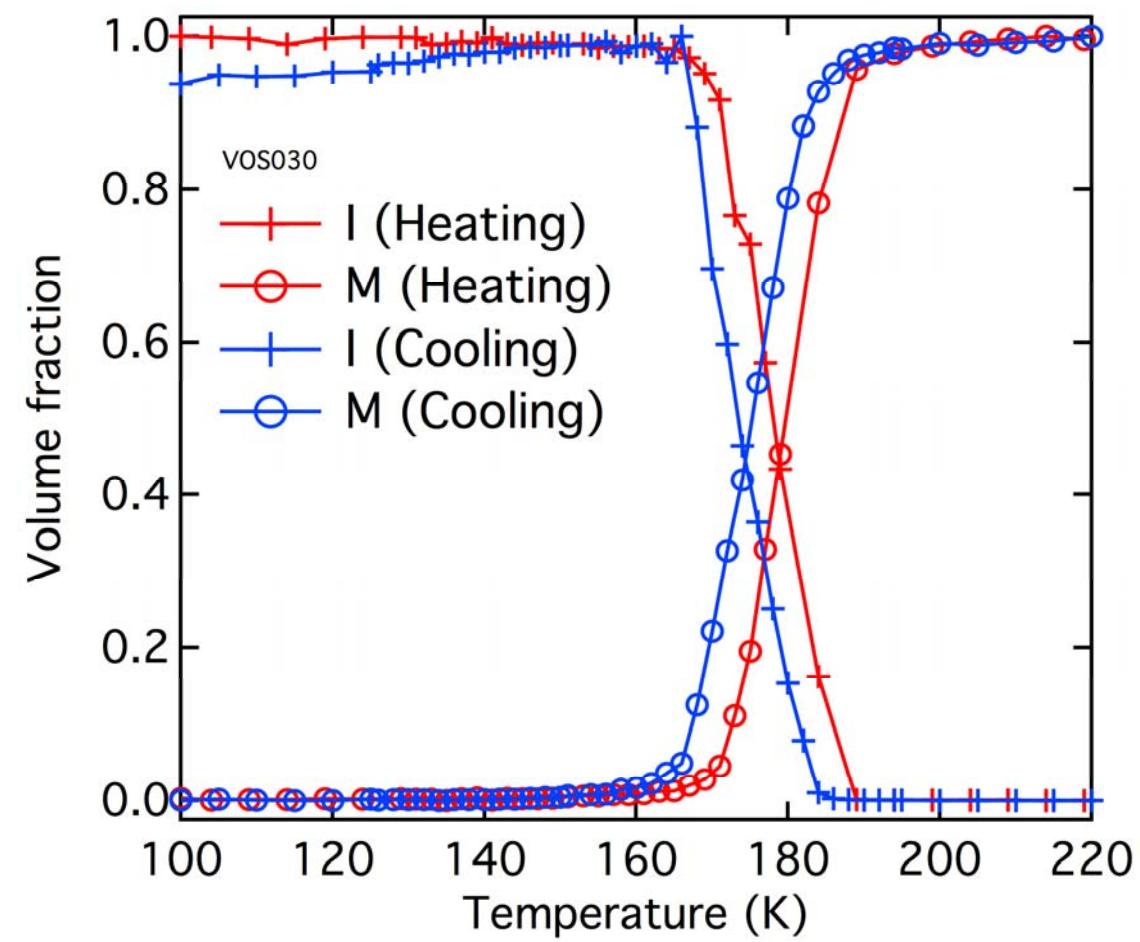
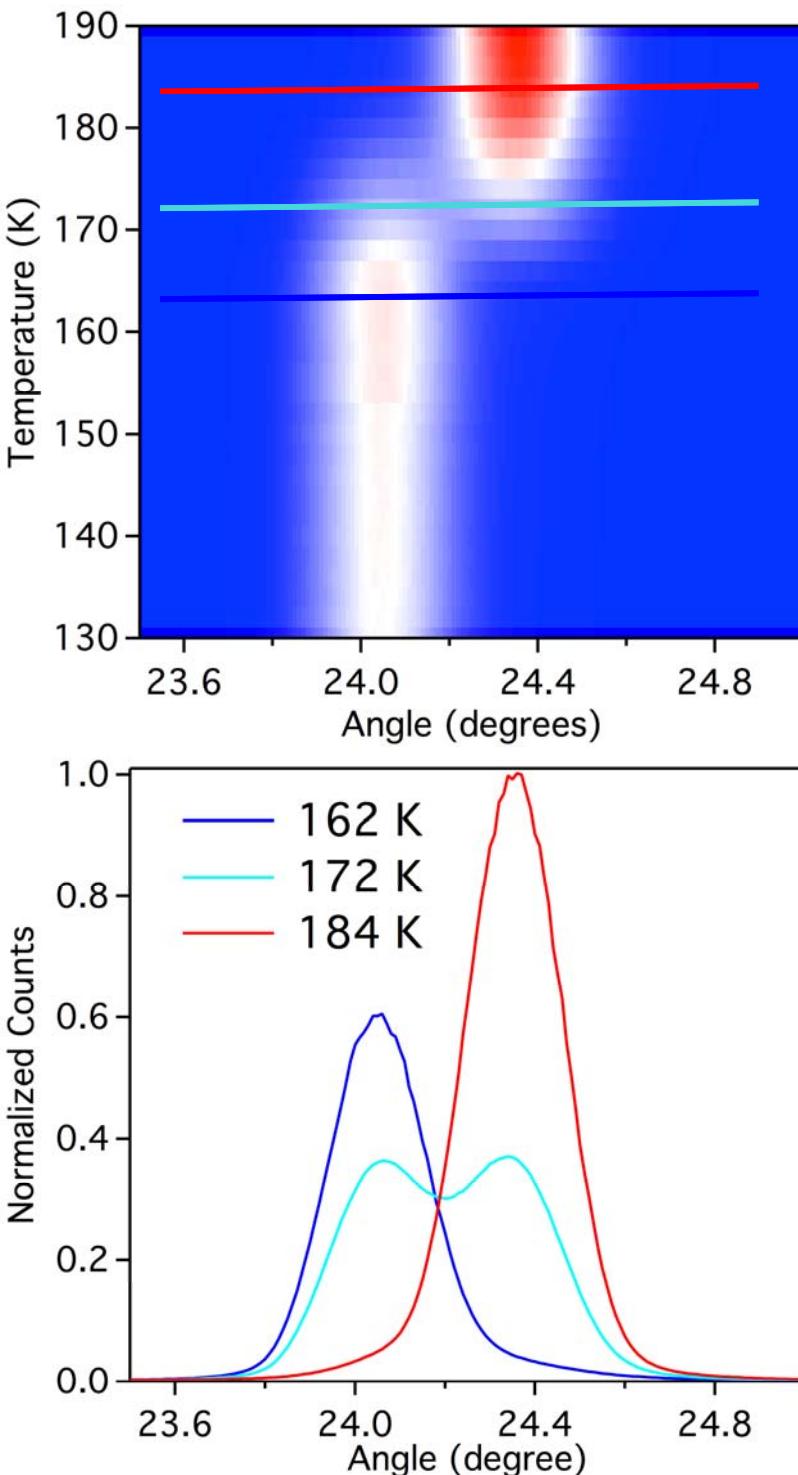
$$E_s = E_{BG} + E_{NF}$$



How to remove background?



# $V_2O_3$ kristal structuur



Volgen de elektronen de  
kristal structuur?

Wat is het verschil tussen een metaal en een isolator?

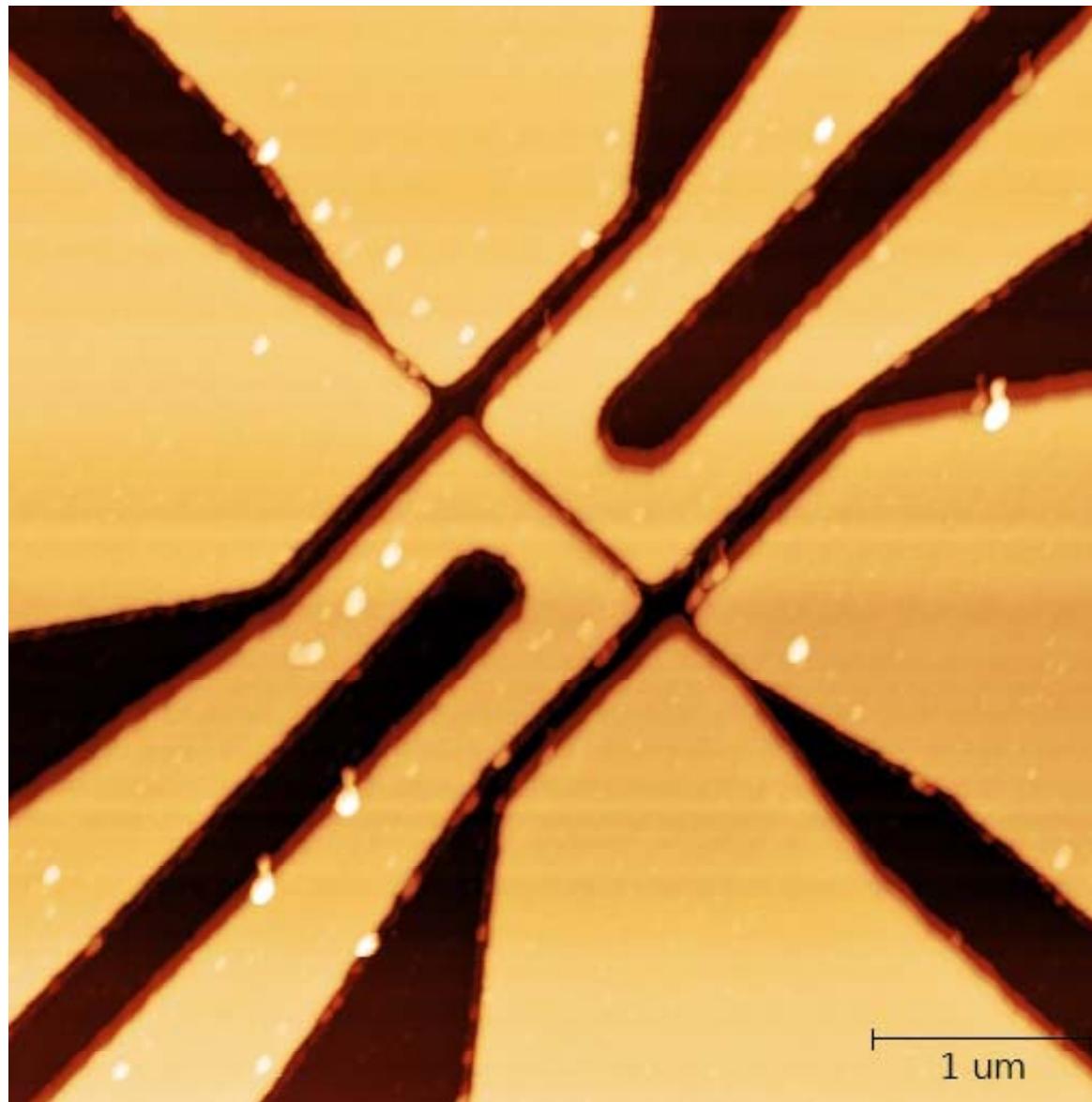


Hoe verandert een metaal in een isolator?

Kan een metaal in een isolator veranderen?

# e-beam lithography

50 nm contact afstand !



# Standard Model of FUNDAMENTAL PARTICLES AND INTERACTIONS

The Standard Model summarizes the current knowledge in Particle Physics. It is the quantum theory that includes the theory of strong interactions (quantum chromodynamics or QCD) and the unified theory of weak and electromagnetic interactions (electroweak). Gravity is included on this chart because it is one of the fundamental interactions even though not part of the "Standard Model."

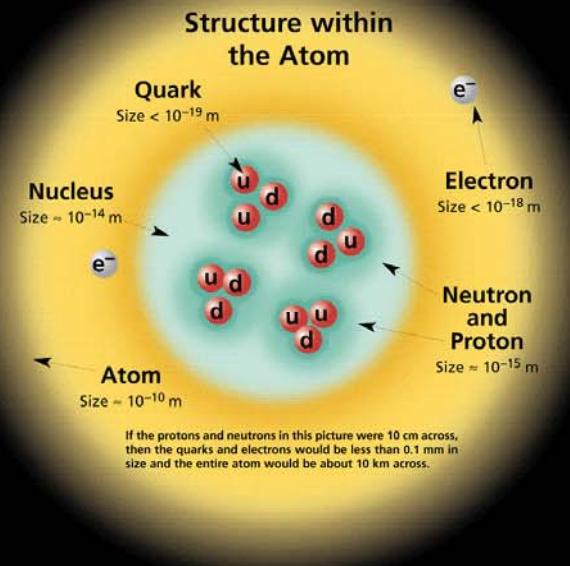
## FERMIONS

matter constituents  
 $spin = 1/2, 3/2, 5/2, \dots$

Leptons spin = 1/2		
Flavor	Mass GeV/c <sup>2</sup>	Electric charge
$\nu_e$ electron neutrino	$<1 \times 10^{-8}$	0
e electron	0.000511	-1
$\nu_\mu$ muon neutrino	$<0.0002$	0
$\mu$ muon	0.106	-1
$\nu_\tau$ tau neutrino	$<0.02$	0
$\tau$ tau	1.7771	-1

Quarks spin = 1/2

Flavor	Approx. Mass GeV/c <sup>2</sup>	Electric charge
u up	0.003	2/3
d down	0.006	-1/3
c charm	1.3	2/3
s strange	0.1	-1/3
t top	175	2/3
b bottom	4.3	-1/3



## BOSONS

force carriers  
 $spin = 0, 1, 2, \dots$

Unified Electromagnetic spin = 1

Name	Mass GeV/c <sup>2</sup>	Electric charge
$\gamma$ photon	0	0
W <sup>-</sup>	80.4	-1
W <sup>+</sup>	80.4	+1
Z <sup>0</sup>	91.187	0

Color Charge  
Each quark carries one of three types of "strong charge," also called "color charge." These charges have nothing to do with the colors of visible light. There are eight possible types of color charge for gluons. Just as electrically-charged particles interact by exchanging photons, in strong interactions color-charged particles interact by exchanging gluons. Leptons, photons, and W and Z bosons have no strong interactions and hence no color charge.

### Quarks Confined in Mesons and Baryons

One cannot isolate quarks and gluons; they are confined in color-neutral particles called **hadrons**. This confinement (binding) results from multiple exchanges of gluons among the color-charged constituents. As color-charged particles (quarks and gluons) move apart, the energy in the color-force field between them increases. This energy eventually is converted into additional quark-antiquark pairs (see figure below). The quarks and antiquarks then combine into hadrons; these are the particles seen to emerge. Two types of hadrons have been observed in nature: **mesons**  $q\bar{q}$  and **baryons**  $qqq$ .

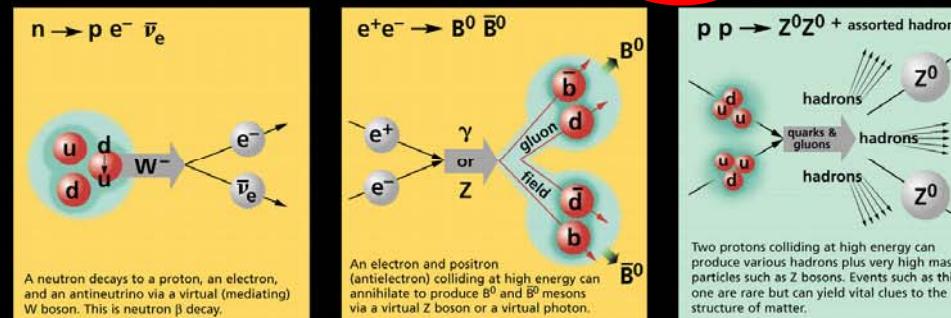
### Residual Strong Interaction

The strong binding of color-neutral protons and neutrons to form nuclei is due to residual strong interactions between their color-charged constituents. It is similar to the residual electrical interaction that binds electrically neutral atoms to form molecules. It can also be viewed as the exchange of mesons between the hadrons.

## PROPERTIES OF THE INTERACTIONS

Baryons $qqq$ and Antibaryons $\bar{q}\bar{q}\bar{q}$					
Baryons are fermionic hadrons. There are about 120 types of baryons.					
Symbol	Name	Quark content	Electric charge	Mass GeV/c <sup>2</sup>	Spin
p	proton	uud	1	0.938	1/2
$\bar{p}$	anti-proton	$\bar{u}\bar{u}\bar{d}$	-1	0.938	1/2
n	neutron	udd	0	0.940	1/2
$\Lambda$	lambda	uds	0	1.116	1/2
$\Omega^-$	omega	sss	-1	1.672	3/2

Property	Interaction		Gravitational	Weak	Electromagnetic (Electroweak)	Fundamental	Strong
	Acts on:	Particles experiencing:	Mass - Energy	Flavor	Electric Charge		
		All	Graviton (not yet observed)	Quarks, Lepton	Electrically charged	Quarks, Gluons	Hadrons
	Particles mediating:	$W^+ W^- Z$			$\gamma$	Gluons	Mesons
	Strength relative to electromagnetism for two u quarks at: 10 <sup>-18</sup> m	10 <sup>-41</sup>	0.8	1	1	25	Not applicable to quarks
	for two protons in nucleus: 3x10 <sup>-17</sup> m	10 <sup>-41</sup>	10 <sup>-4</sup>	1	1	60	20
		10 <sup>-36</sup>	10 <sup>-7</sup>	1	1	Not applicable to hadrons	



Mesons $q\bar{q}$					
Mesons are bosonic hadrons. There are about 140 types of mesons.					
Symbol	Name	Quark content	Electric charge	Mass GeV/c <sup>2</sup>	Spin
$\pi^+$	pion	u $\bar{d}$	+1	0.140	0
K <sup>-</sup>	kaon	s $\bar{u}$	-1	0.494	0
$\rho^+$	rho	u $\bar{d}$	+1	0.770	1
$B^0$	B-zero	d $\bar{b}$	0	5.279	0
$\eta_c$	eta-c	c $\bar{c}$	0	2.980	0

### The Particle Adventure

Visit the award-winning web feature *The Particle Adventure* at <http://ParticleAdventure.org>

This chart has been made possible by the generous support of:

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### Figures

These diagrams are an artist's conception of physical processes. They are not exact and have no meaningful scale. Green shaded areas represent the cloud of gluons or the gluon field, and red lines the quark paths.

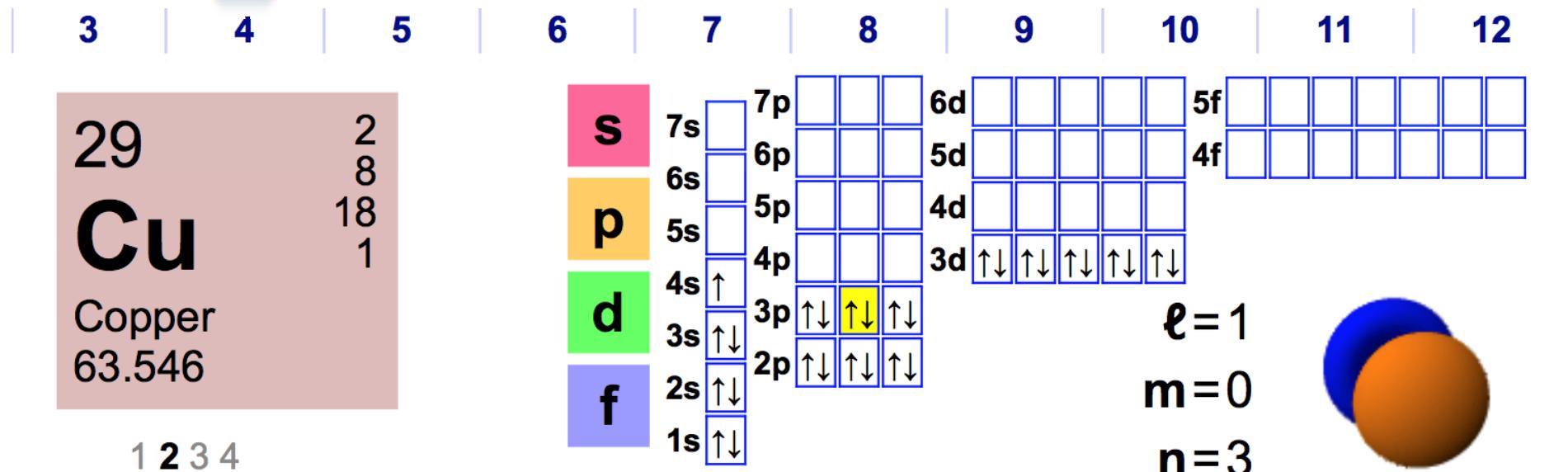
## Hoe verandert een metaal in een isolator?



Elektronen zijn fermionen.



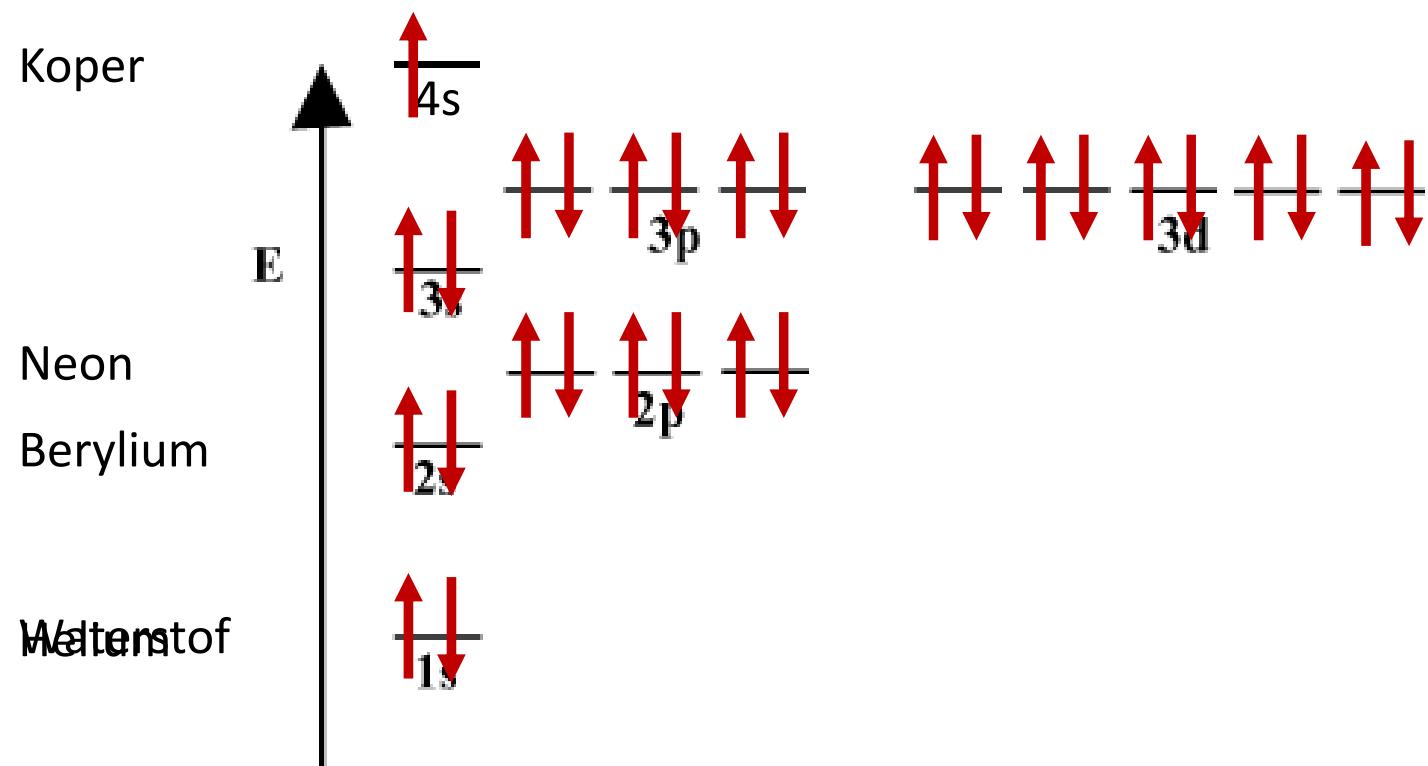
Ze wisselwerken via de Coulomb interactie.



<b>21</b> <b>Sc</b> Scandium 3	<b>22</b> <b>Ti</b> Titanium 4	<b>23</b> <b>V</b> Vanadium 5	<b>24</b> <b>Cr</b> Chromium 3,6	<b>25</b> <b>Mn</b> Manganese 2,4,7	<b>26</b> <b>Fe</b> Iron 2,3	<b>27</b> <b>Co</b> Cobalt 2,3	<b>28</b> <b>Ni</b> Nickel 2	<b>29</b> <b>Cu</b> Copper 2	<b>30</b> <b>Zn</b> Zinc 2
<b>39</b> <b>Y</b> Yttrium 3	<b>40</b> <b>Zr</b> Zirconium 4	<b>41</b> <b>Nb</b> Niobium 5	<b>42</b> <b>Mo</b> Molybdenum 4,6	<b>43</b> <b>Tc</b> Technetium 4,7	<b>44</b> <b>Ru</b> Ruthenium 3,4	<b>45</b> <b>Rh</b> Rhodium 3	<b>46</b> <b>Pd</b> Palladium 2,4	<b>47</b> <b>Ag</b> Silver 1	<b>48</b> <b>Cd</b> Cadmium 2



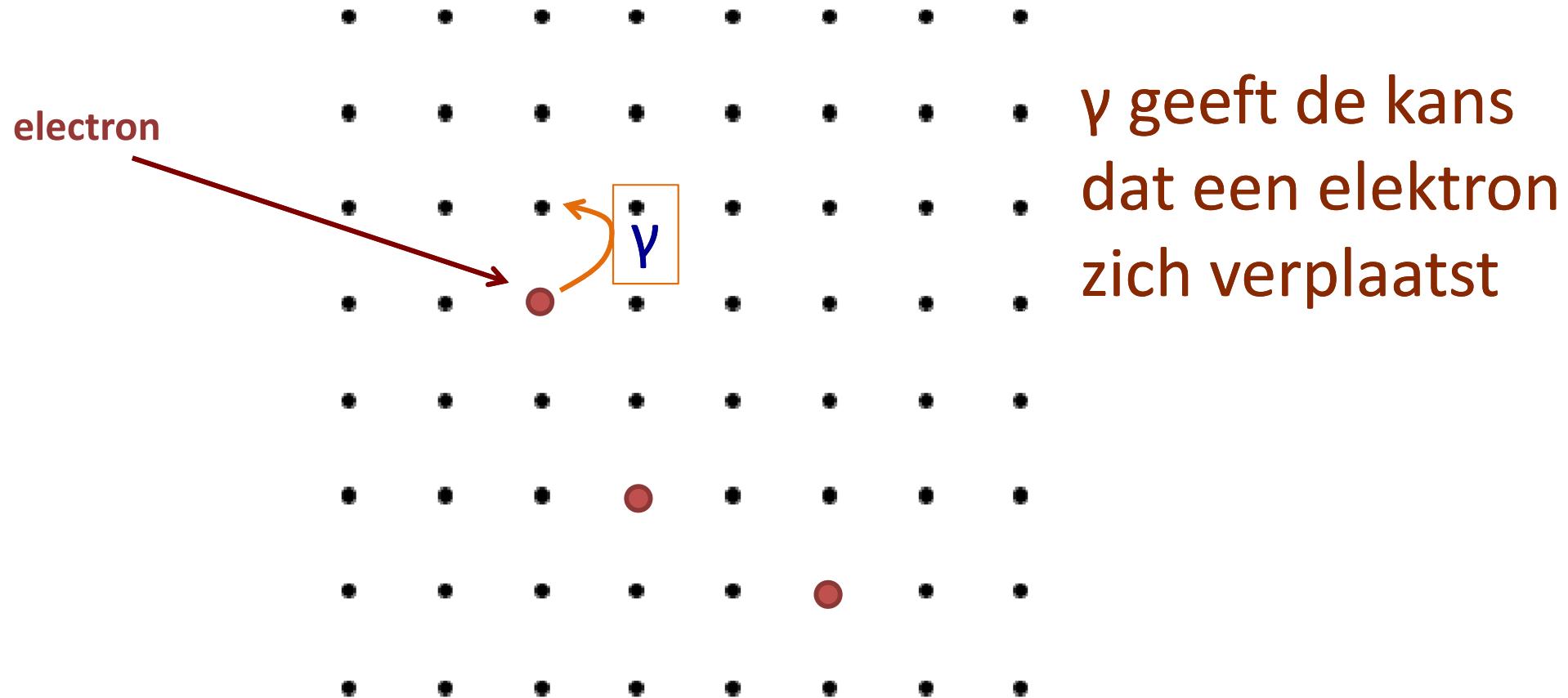
## Hoe verandert een metaal in een isolator?



# — Model voor een metaal —



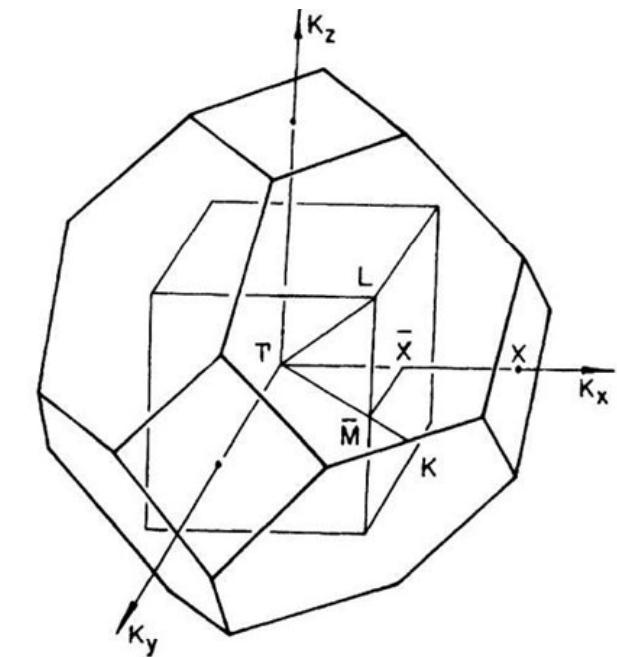
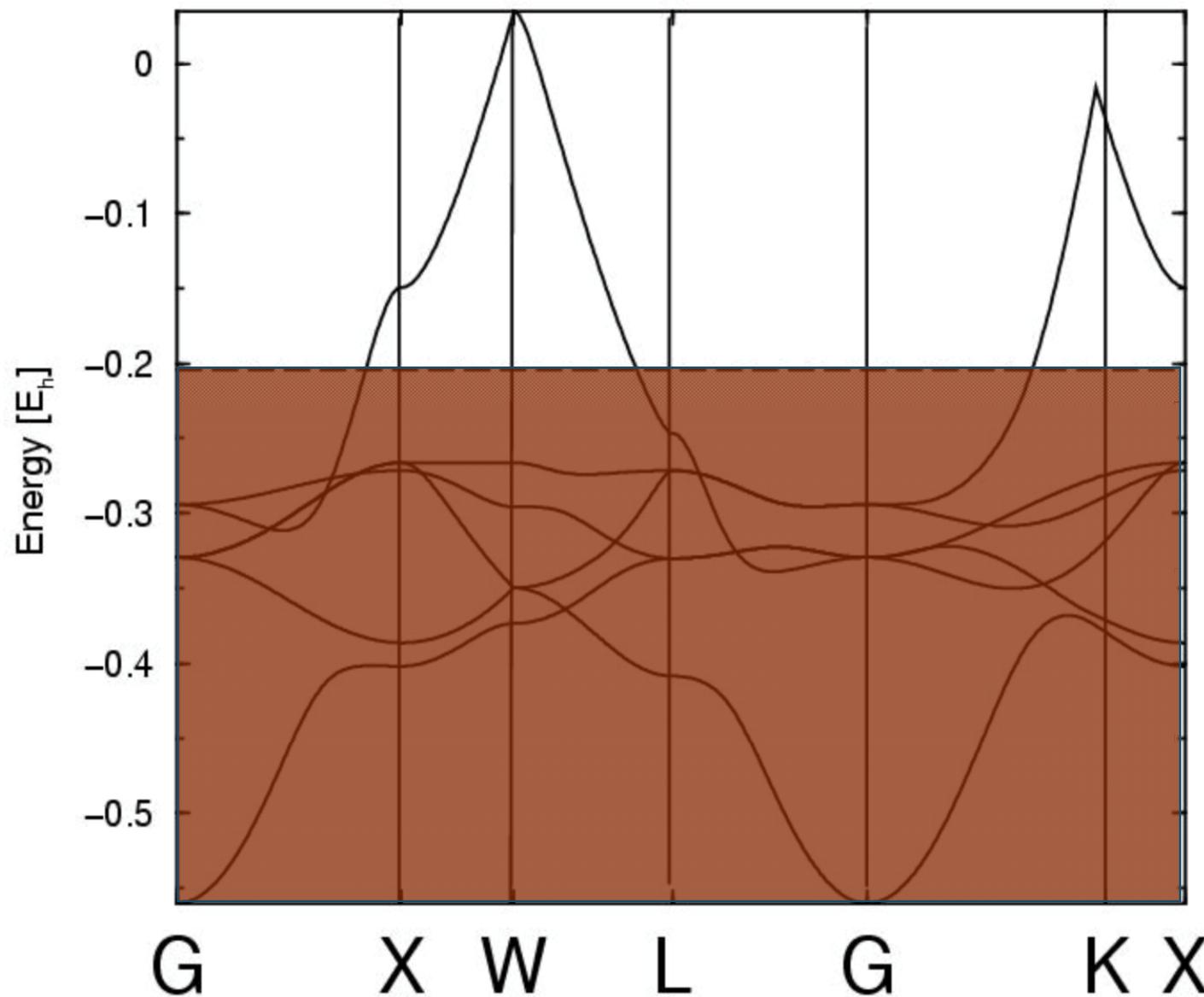
Neem een rooster van atomen.



# Model voor een metaal –

Koper

LDA band structure



# Het Hubbard model

- Het simpelste model voor wisselwerkende elektronen.

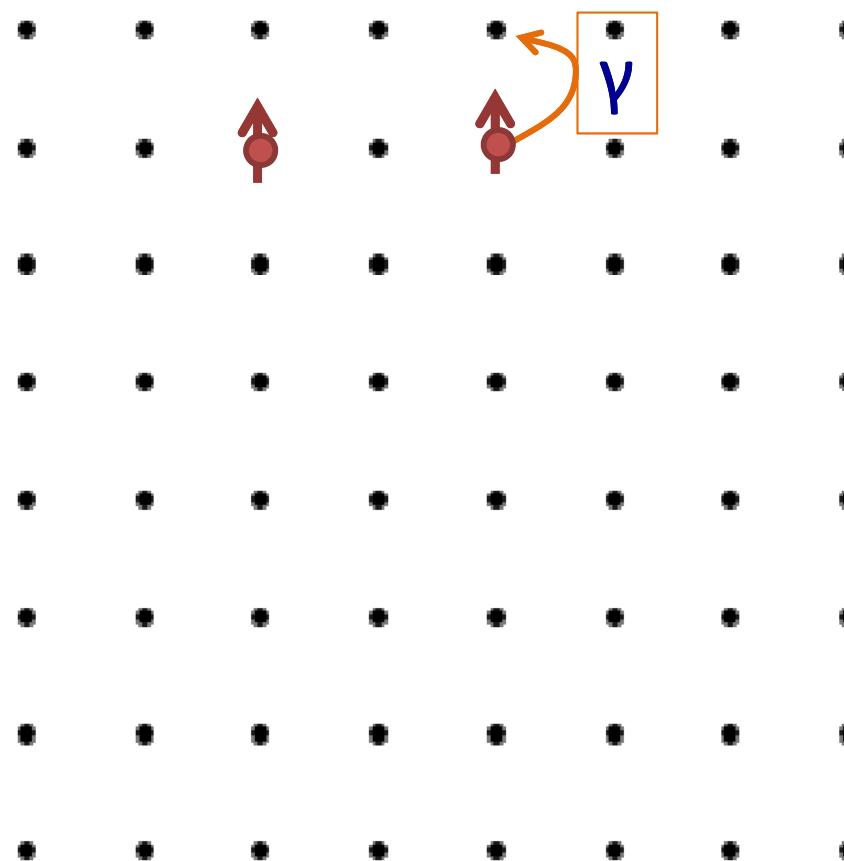
$$H_{int} = \begin{cases} U & e_1 \text{ en } e_2 \text{ op hetzelfde roosterpunt} \\ 0 & e_1 \text{ en } e_2 \text{ niet op hetzelfde punt} \end{cases}$$

- Twee fermionen kunnen alleen op hetzelfde roosterpunt zijn als hun spin anti-parallel is.

# The Hubbard model



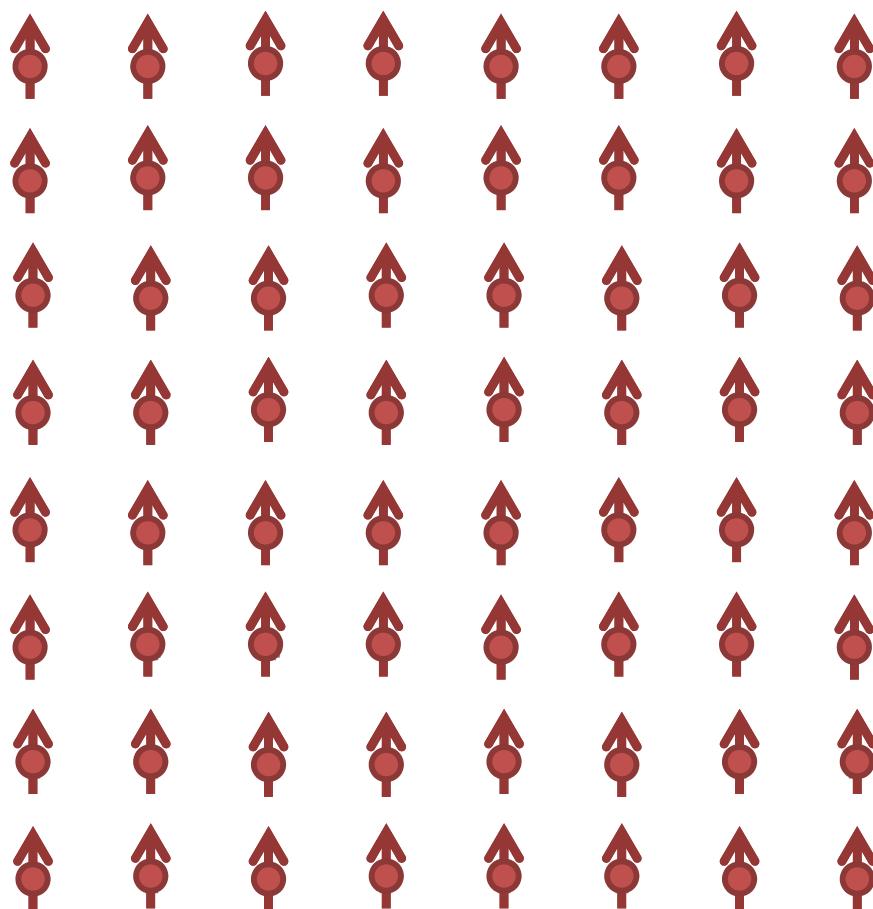
Neem een rooster van atomen.



# The Hubbard model



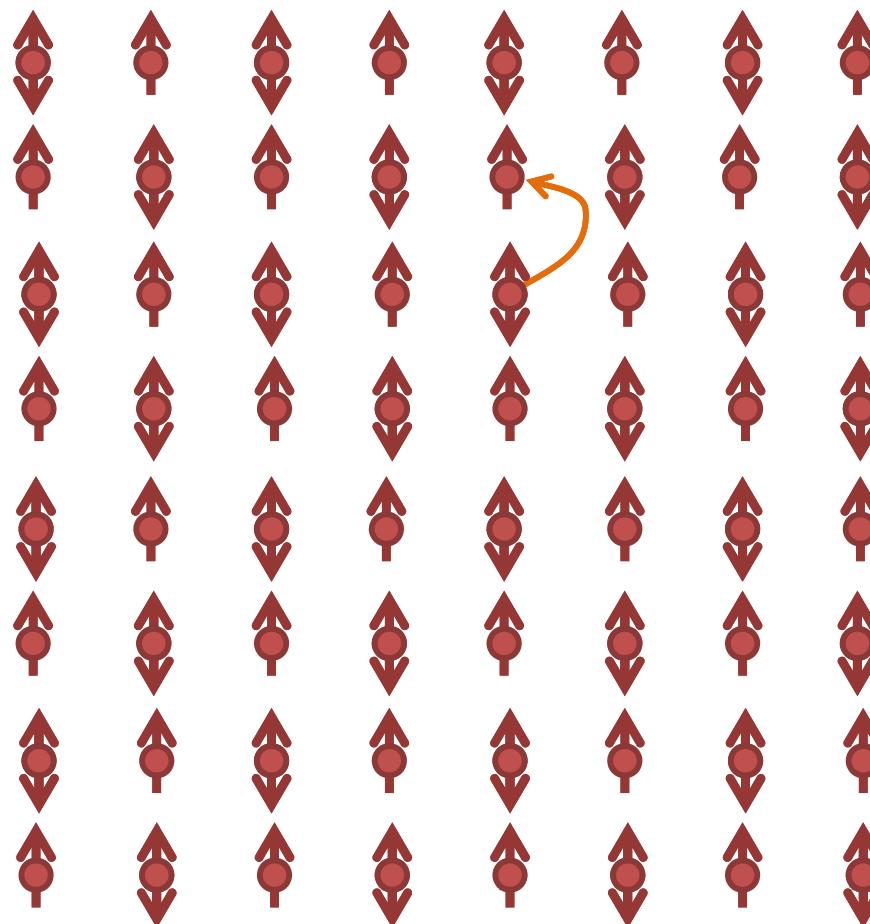
Neem een rooster van atomen.



# The Hubbard model



Als alle spins dezelfde kant opstaan,  
zitten de elektronen vast!

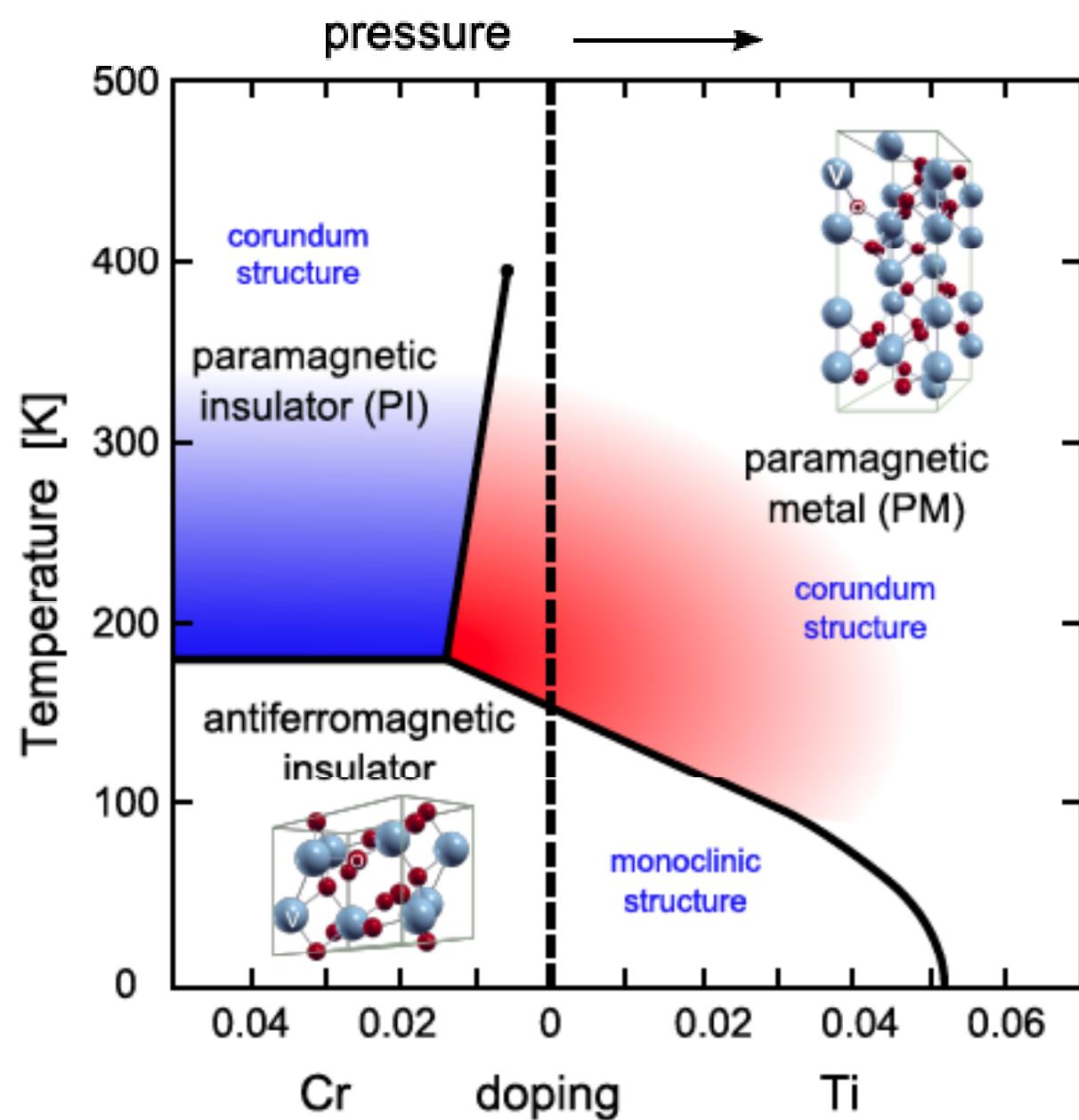


Mott-Hubbard  
isolator



Met anti-parallelle spins winnen ze  $E_{kin}$

# Metaal-Isolator overgang in $V_2O_3$



Sterk wisselwerkend metaal

Structurele en magnetische overgangen

Wat drijft de overgang van metaal naar isolator?

McWhan et al., PRL 23, 1384 (1969)

Hansmann et al. Phys. Status Solidi B 250, 1251 (2013)